

Artificial neural networks and superconducting basic  
elements beyond von Neumann computer  
Superconducting neural networks for broadband signal  
receiving and processing

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Automatics

# State of the Art

## Artificial Neural Networks

hardware

software



ANN

1) clustering

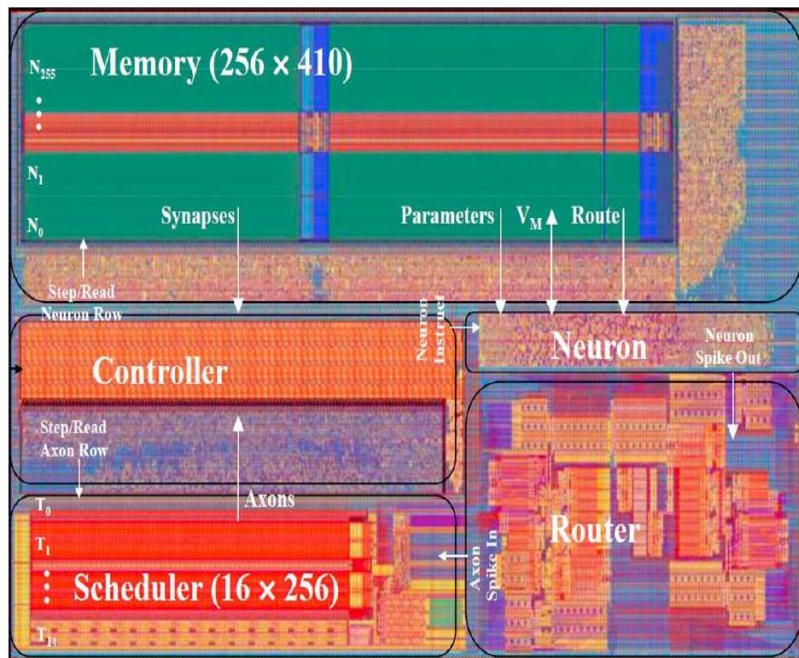


2) recognition



As well as:  
3) forecasting  
4) approximation  
5) optimization

Synaptic chip IBM (TrueNorth)



Increase energy efficiency and speed!

# Relevance

Adiabatic superconducting logic demonstrates the highest energy efficiency

Orbital satellite communication system



Reception and processing of weak broadband signals



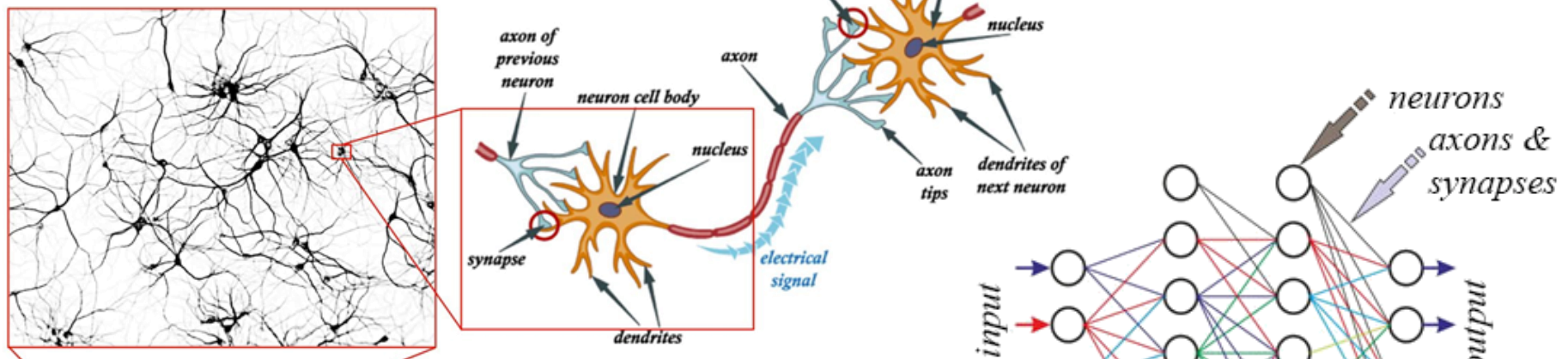
An adiabatic superconducting processor was created that consumes 15 fJ at clock speeds of 5 GHz

Deep space exploration

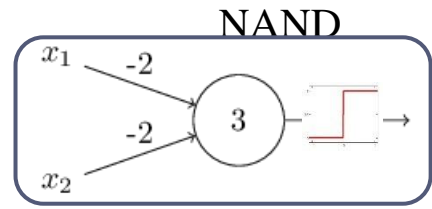
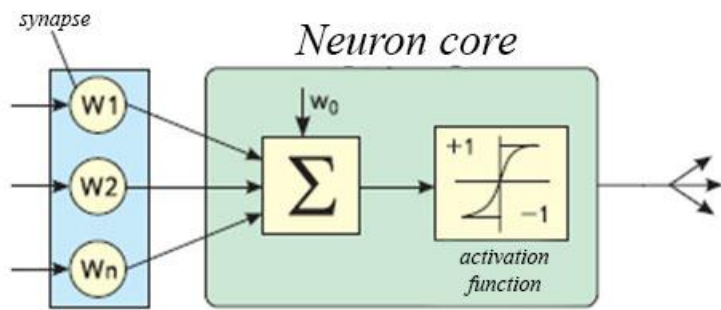


Physical problem statement: investigation of the adiabatic evolution of systems based on the S-quantron for the construction of an energy-efficient element base of the SNN.

# Subject: physical implementation of neurons and connections



humans don't need features  
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analog

digital

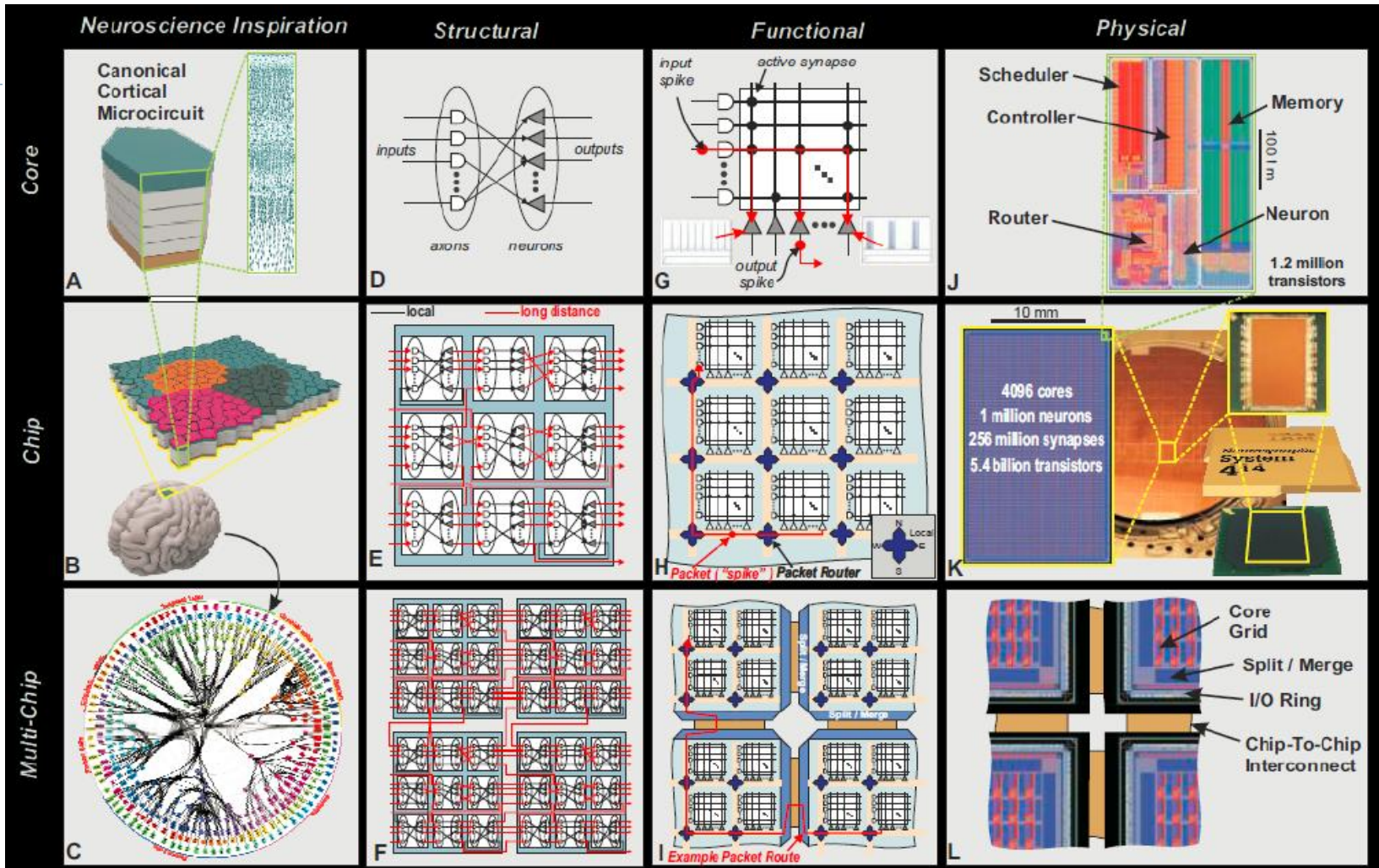
IBM TrueNorth (1M neurons, 256M synapses)  
 Intel Loihi (130K neurons, 130M synapses)

Google TPU (105 x 4 = 420 TFLOS)  
 Huawei Ascend 910 (256 TFLOPS [FP16], 512 TOPS (INT8))



# IBM TrueNorth

- Science 345, 668 (2014)
- Front Neurosci. 9, 141 (2015)

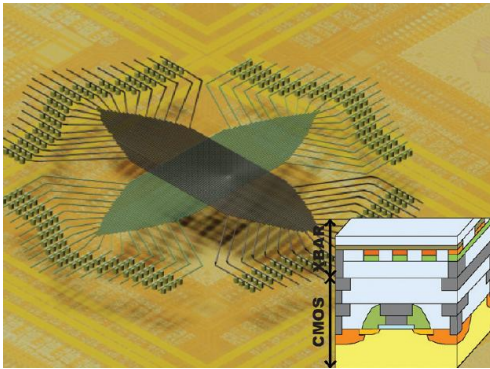


1M neurons  
256M synapses, ~ 400 Mbit SRAM  
46 x 10<sup>9</sup> OPS (70 - 100 mW)

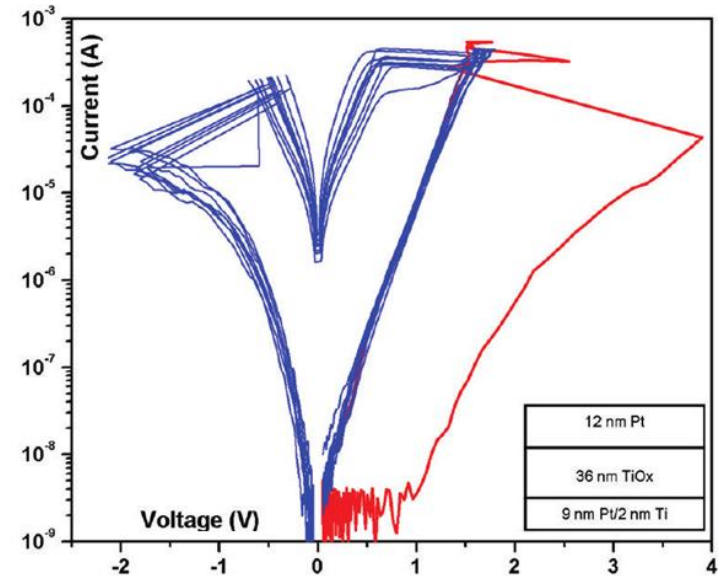
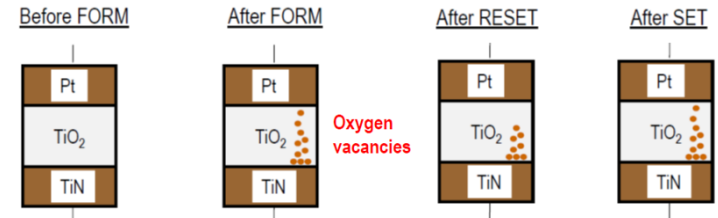
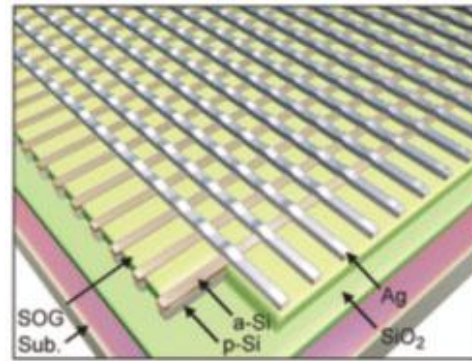
4096 cells (64 x 64)  
100 Kbit SRAM for synapse memory (2 bits/synapse)  
256 neurons ( $f_c = 1$  KGz)

# Memristors

## CMOS + Memristors



## top grid

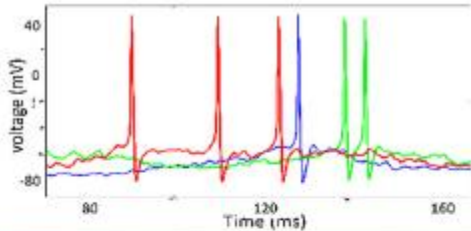
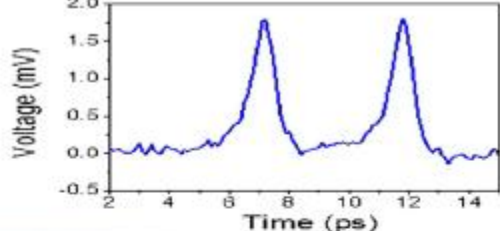

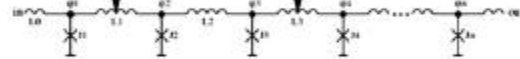
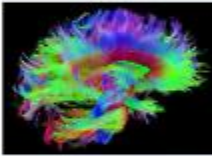
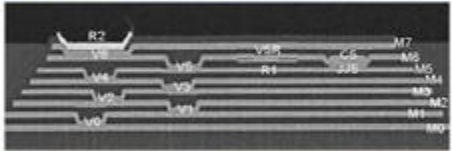
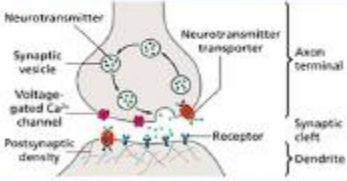



	ITRI, IEDM 2008	NEC, VLSI 2010	Panasonic, IEDM 2008	Univ. + IMEC, IMW 2010	Fujitsu, IEDM 2007
Device	TiN/Ti/HfO <sub>x</sub> /TiN	Ru/TiO <sub>x</sub> /TaO <sub>x</sub> /Ru	Pt/TaO <sub>x</sub> /Pt	Au/NiO <sub>x</sub> /TiN	Pt/Ti-doped NiO/Pt
Reset	2V, 25uA	0.65V, 200uA	1.5V, 100uA	0.5V DC, 9.5uA	1.9V, 100uA
Set	2.3V	2.8V	2V	2.7V DC	2.8V
Form Voltage	3V	?	?	3.7V DC	3V
Switching Time	<10ns	<1us	<100ns	NA	10ns

$P \sim 10^{-4} \text{ W}$



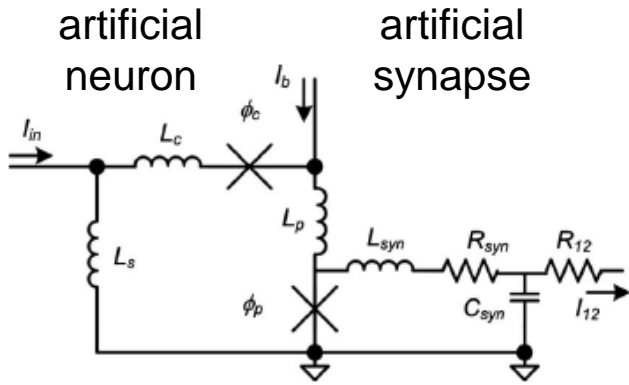
# ANN implementation

	<b>Neural</b>	<b>Single Flux Quantum</b>
a) Information transfer: quantized pulse trains		
b) Long distance "lossless" pulse transmission		
c) 3D architecture	 White matter neural tracks	
d) Memory/ plasticity	 synapse	 magnetic Josephson junction
e) Number of neurons/fanout	$10^{11}$ / 1000	$10^7$ / 100
f) Speed (pulses/neuron/s)	$10^3$	$10^{10}$
g) Power	20 W	0.1 mW

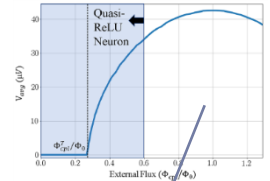
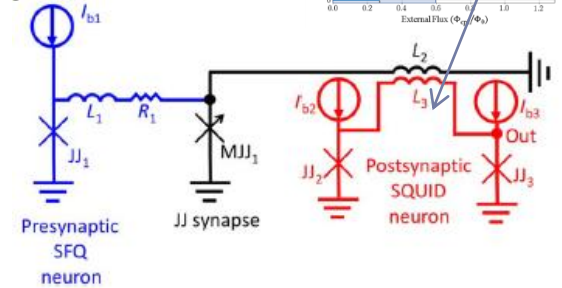
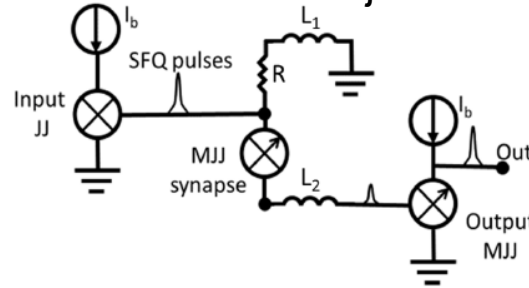
- M.L. Schneider et al., J. Appl. Phys. 124, 161102 (2018)



# SFQ-based ANNs



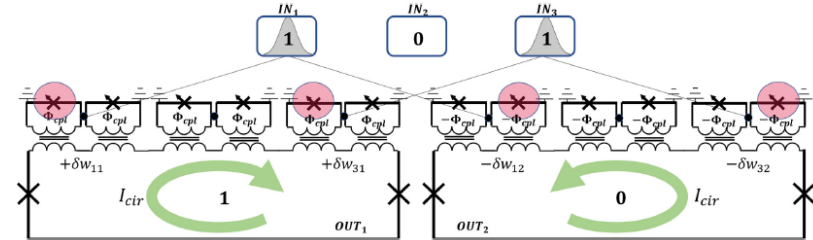
MJJ based artificial synapse with adjustable weight



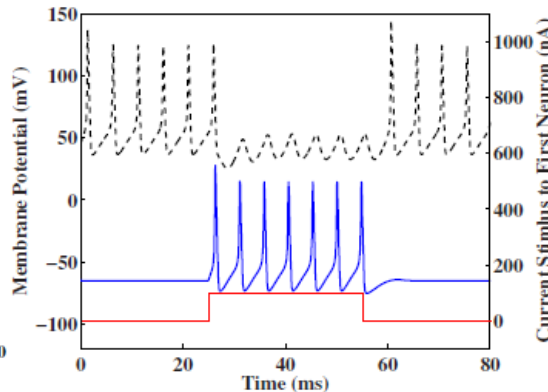
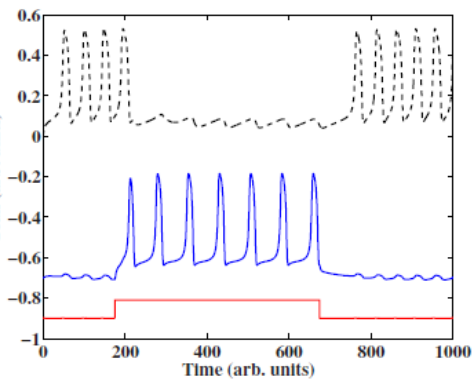
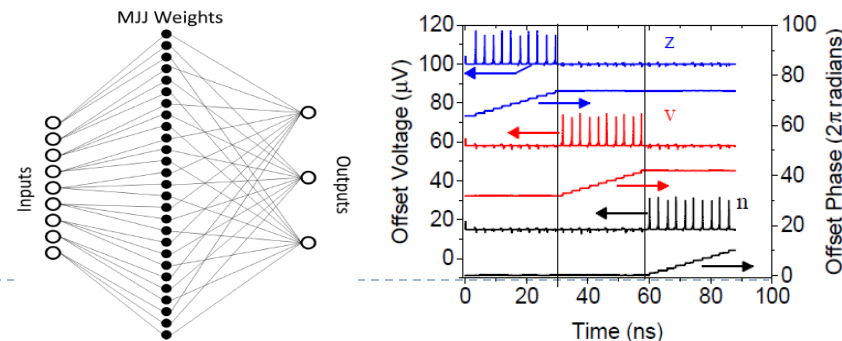
Inhibitory synaptic coupling of two SFQ-based neurons

Behavior of two Hodgkin-Huxley neurons coupled with an inhibitory synapse model

Synaptic connections with neurons



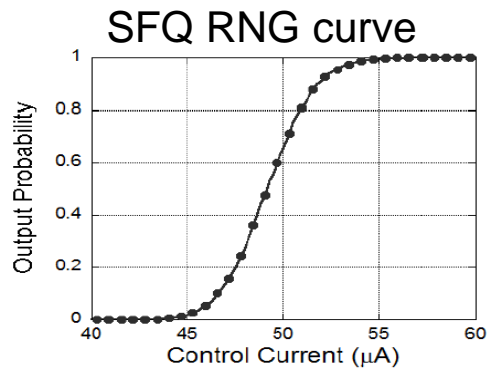
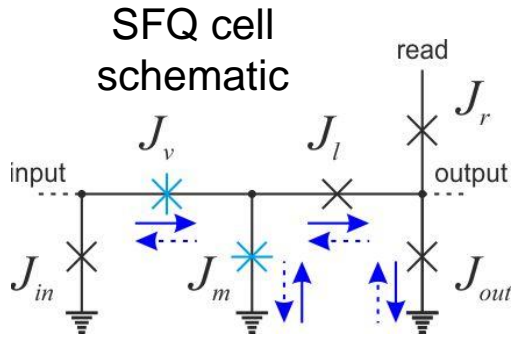
Example of operation



- P. Crotty et al., Phys. Rev. E 82, 011914 (2010)
- M.L. Schneider et al., IEEE ICRC, 17413500 (2017)
- M.L. Schneider et al., Sci. Adv. 4, e1701329 (2018)
- M.L. Schneider et al., J. Appl. Phys. 124, 161102 (2018)



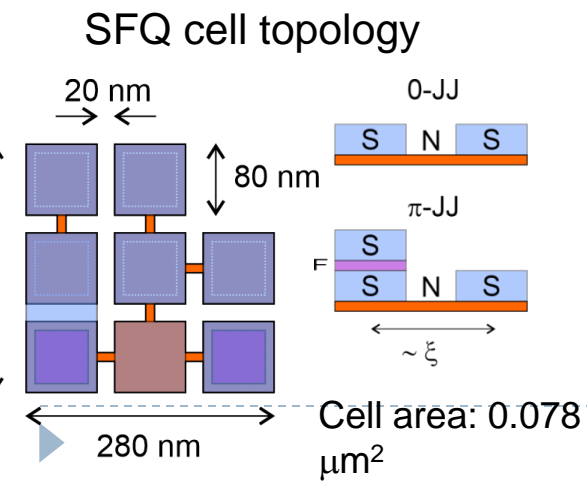
# Superconducting tensor processor unit



## Estimations (SC TPU):

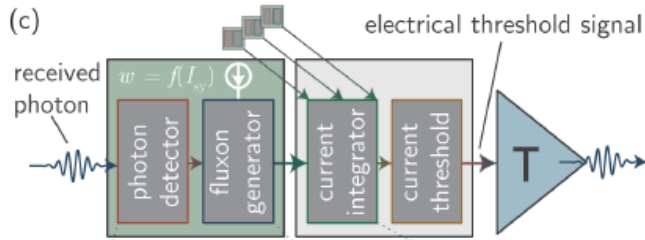
- Stream length = 256
- Cell area with =  $0.3 \times 0.3 \sim 0.1 \mu\text{m}^2$
- ALU area =  $2 \times 256 \times 0.1 \sim 50 \mu\text{m}^2$
- Chip area =  $1 \times 1 \text{ cm}^2 = 10^8 \mu\text{m}^2$
- $2 \times 2 \times 128 \times 128 \sim 65 \times 10^3$  ALUs/chip
- Available memory  $\sim 10^8 / 0.1 = 1$  Gbit/layer
- $f_c = 40$  GHz ( $t_c = 25$  ps)
- $E_{\text{bit}} = 2$  aJ ( $E_{\text{op}} = 2 \times 256 = 512$  aJ):  $E_{\text{SCE}}/E_{\text{CMOS}} \sim 10^{-3}$
- 1 chip = 2 active layers / 2 cores / 2 systolic arrays  
128x128 ALUs
- $2 \times 2 \times 2 \times 128 \times 128 \times 2 \times 40 \times 10^9 = 10.5$  POPS  
( $\sim 40$  POPS four-chip module):  $\text{Th}_{\text{SCE}}/\text{Th}_{\text{CMOS}} \sim 10^2$
- 25 SC TPU  $\sim 1$  EOPS

- ✓ High clock frequency and 3D architecture allow *2 orders of magnitude performance improvement*
- ✓ Low energy dissipation allows *an order of magnitude improvement in energy efficiency* (including a cooling penalty)

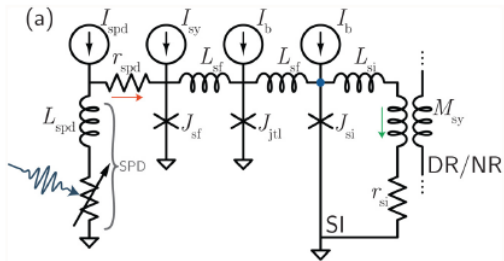


# Superconducting optoelectronic ANN

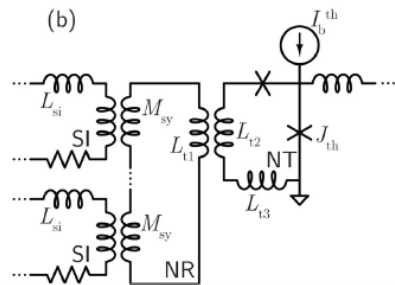
## signal processing



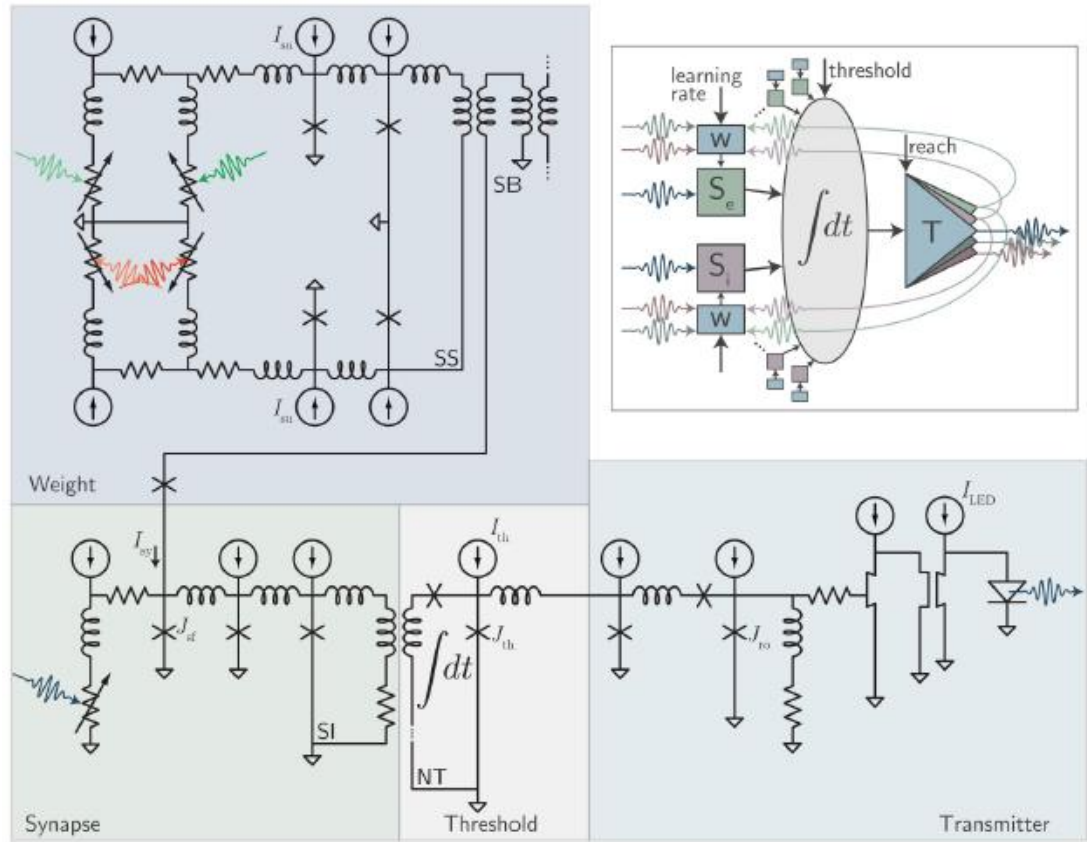
## synaptic connection



## integration and threshold circuits



## neural block with synaptic weight update

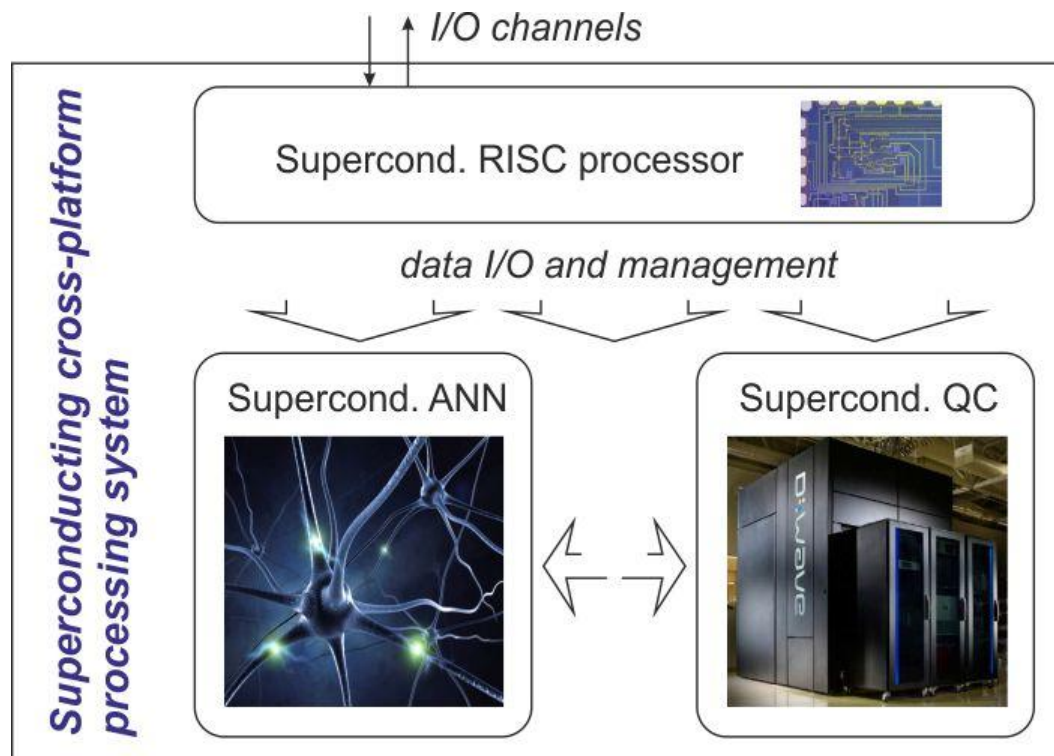


- J. M. Shainline et al., J. Appl. Phys. 124, 152130 (2018)
- J. M. Shainline et al., J. Appl. Phys. 126, 044902 (2019)

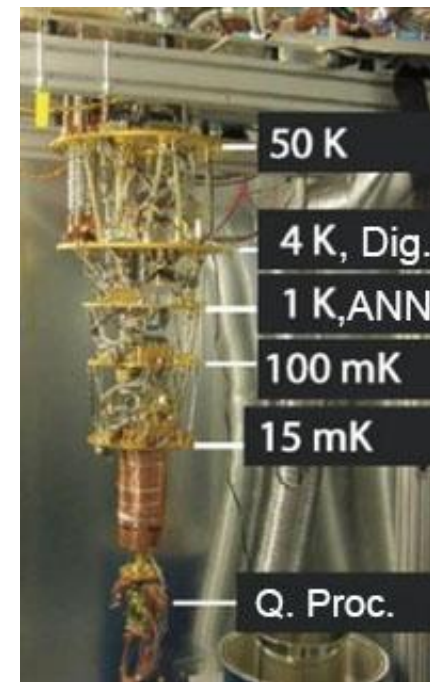


# Superconducting "hybrid" solutions

Fast and energy-efficient platform for quantum and neural network computing



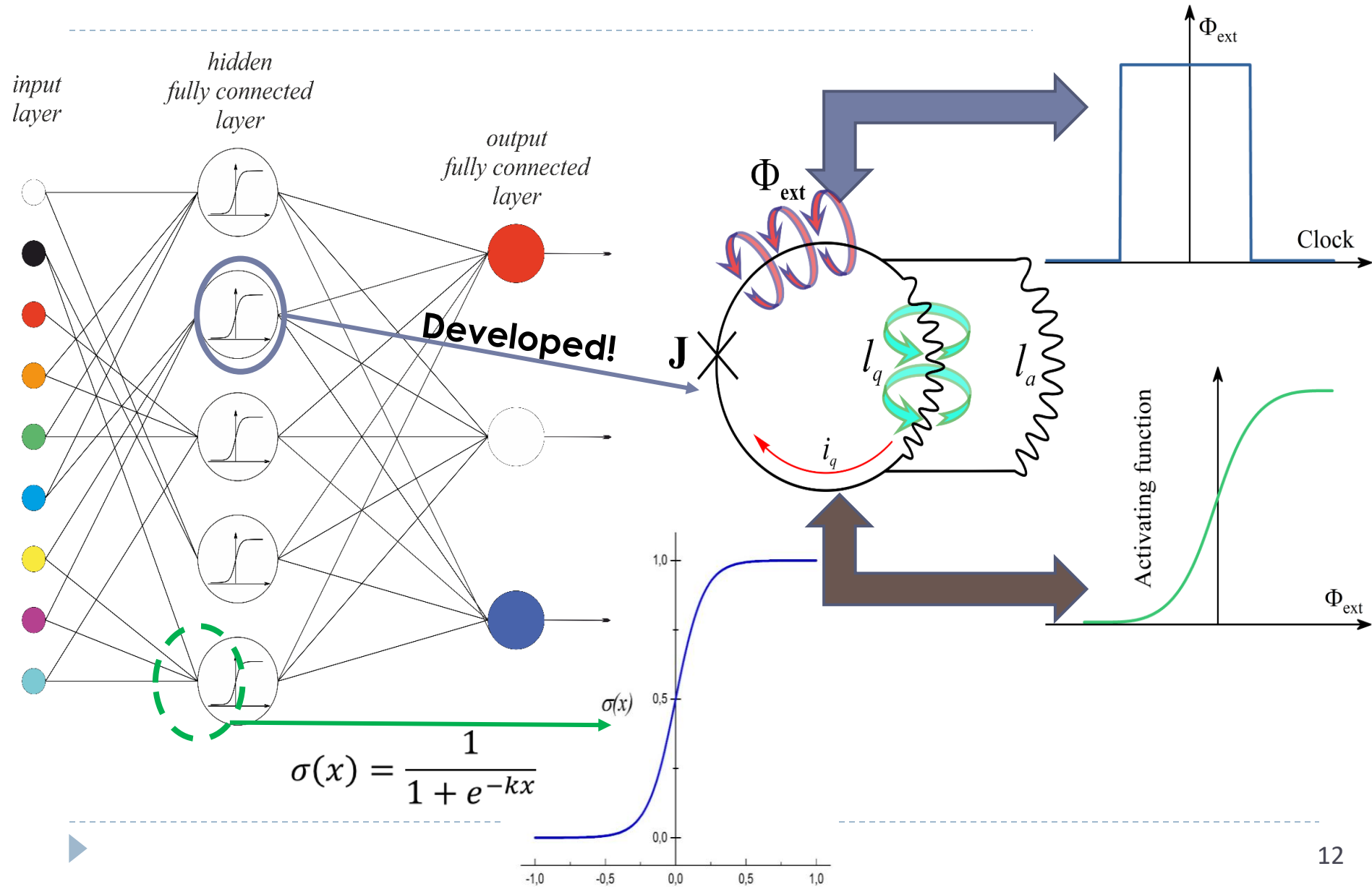
Similar element bases!



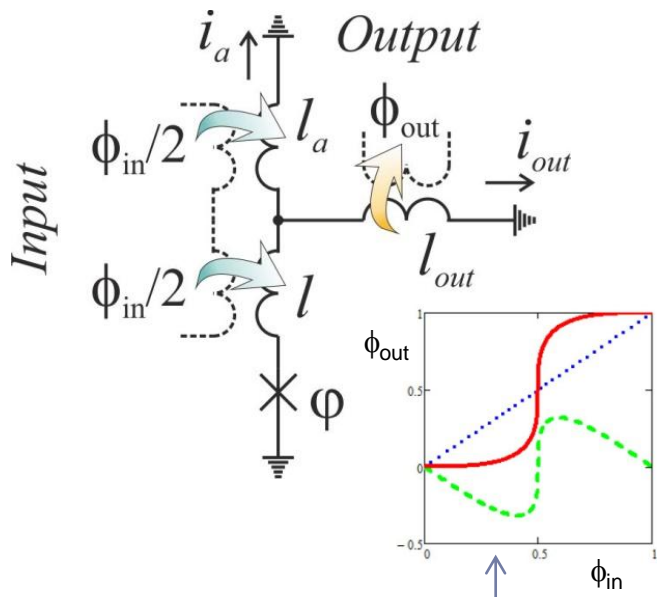
Temperature levels



# Sigma-neuron for perceptron



# Sigma-neuron: main idea



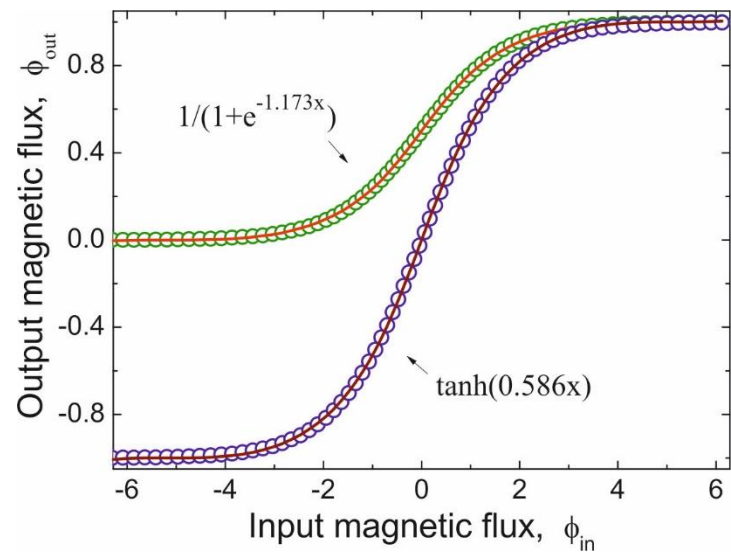
$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

or

$$\tau(x) = \tanh(x)$$

$$l_a = 1 + l.$$

$$l = 0.125, l_{out} = 0.3$$



$$\varphi + l \sin \varphi = \phi_{in} + l_a i_a,$$



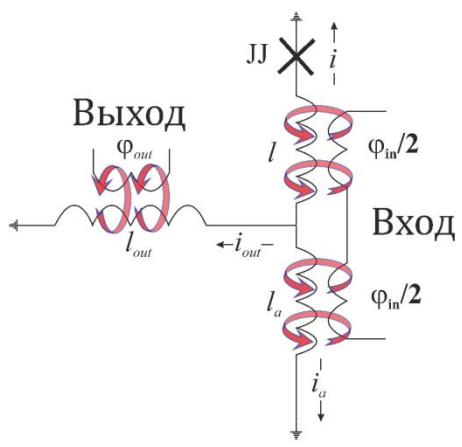
$$\phi_{in} = 2 \left( \frac{l_a + l_{out}}{l_a + 2l_{out}} \right) \left[ \varphi + \left( l + \frac{l_a l_{out}}{l_a + l_{out}} \right) \sin \varphi \right]$$

$$\phi_{out} = l_{out} \frac{\phi_{in} - 2l_a \sin \varphi}{2(l_a + l_{out})}$$

$$\varphi + l \sin \varphi = \phi_{in}/2 + l_{out} i_{out},$$

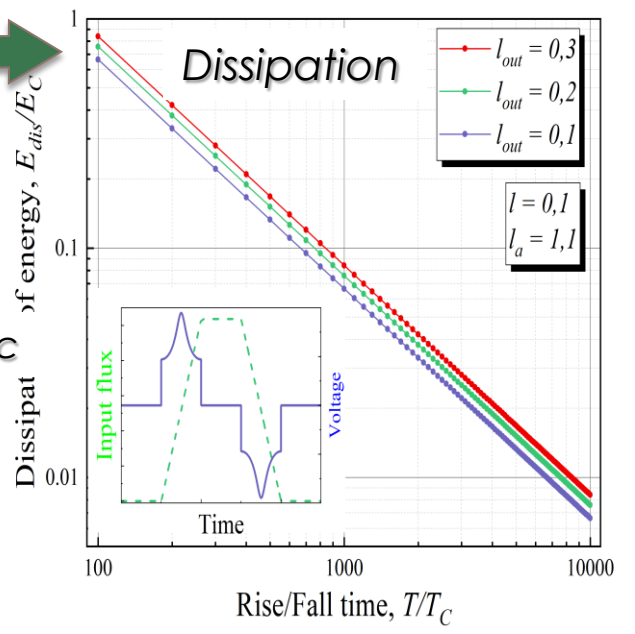
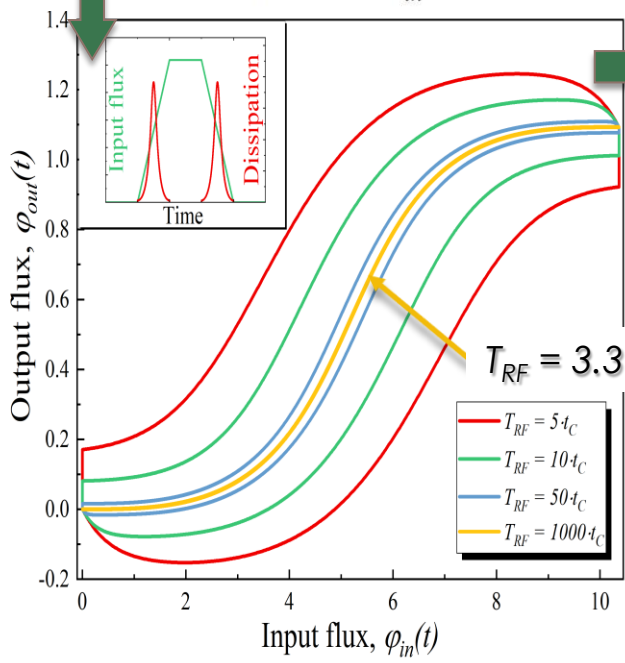
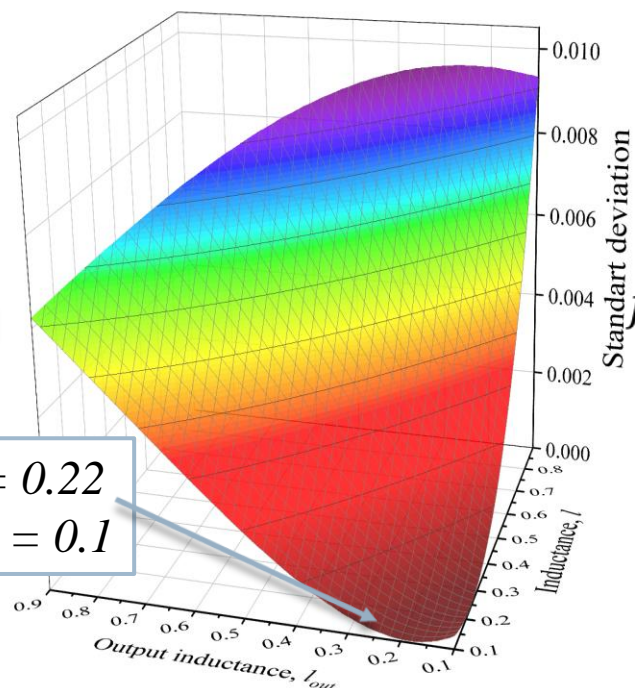
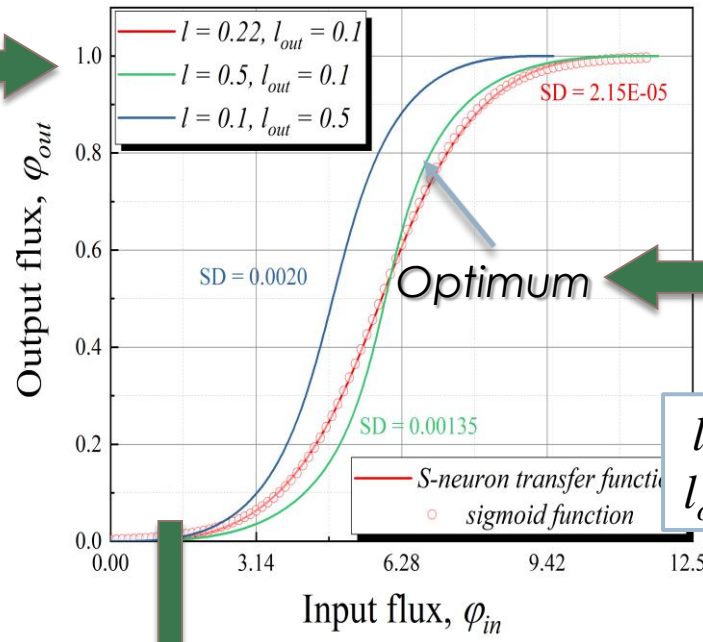
Soloviev I. I., Schegolev A. E., Klenov N. V., Bakurskiy S. V., Kupriyanov M. Y., Tereshonok M. V., Golubov A. A. (2018). Adiabatic superconducting artificial neural network: Basic cells. *Journal of Applied Physics*, 124(15), 152113.

# Sigma-neuron: optimization



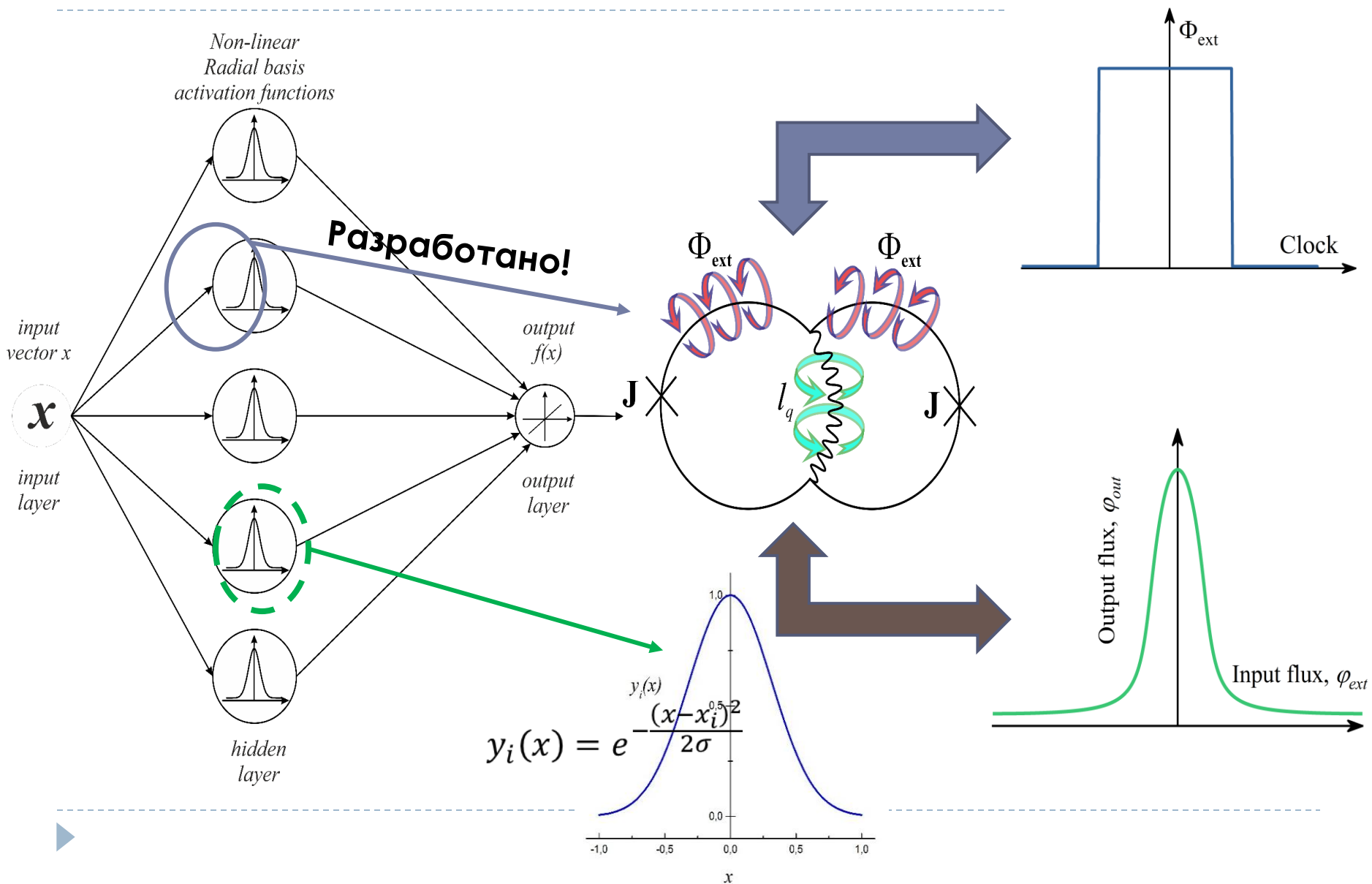
$$\varphi_{out} = l_{out} \frac{\varphi_{in} - 2l_a \sin \varphi}{2(l_a + l_{out})}$$

$I_C = 100 \mu A$     $R_N = 1 \Omega$   
 $T_{RF} = 3.3 \text{ ns}$   
 $E_{dis} \approx 2.6 \times 10^{-21} \text{ J} = 2.6 \text{ zJ}$   
 $(E_L = k_B T \times \ln 2 = 4 \times 10^{-23} \text{ J})$

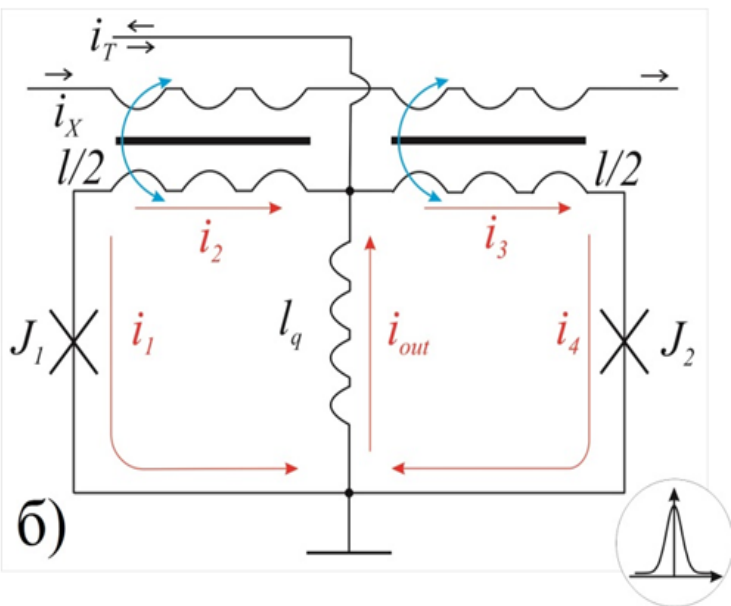




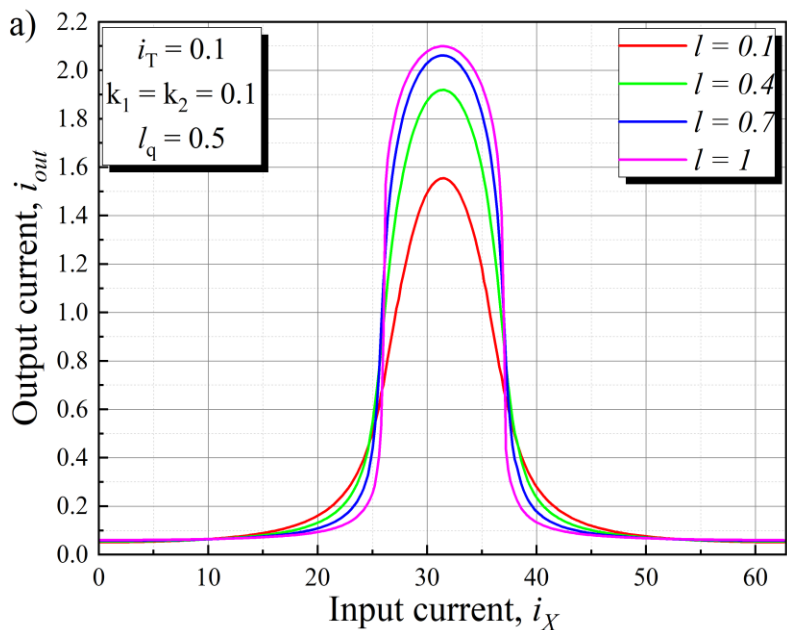
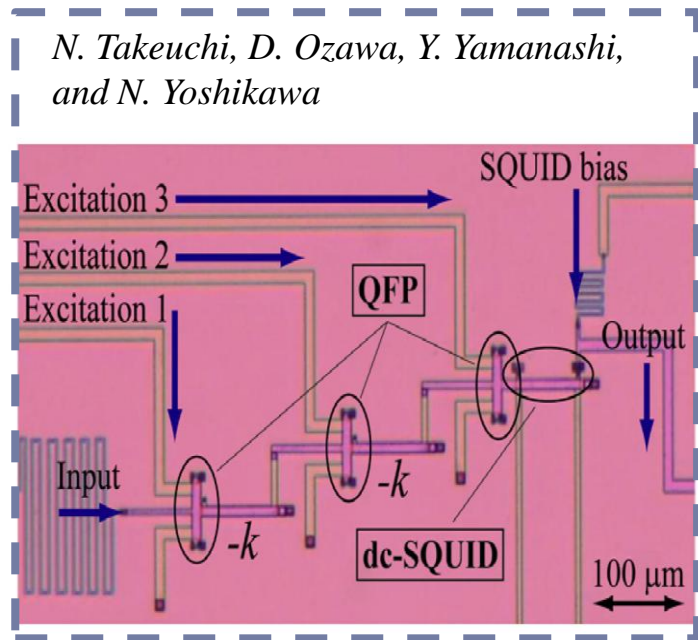
# Gauss-neuron for RBF-network



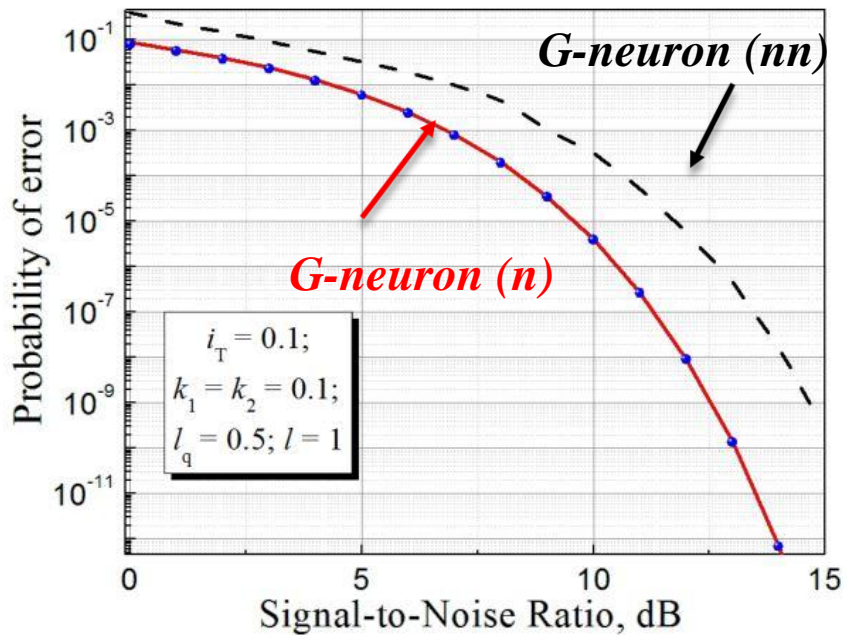
# Gauss-neuron: main idea



$E_{dis} = 10 \text{ zJ}$   
 $t = 0.2 \text{ ns}$



Test

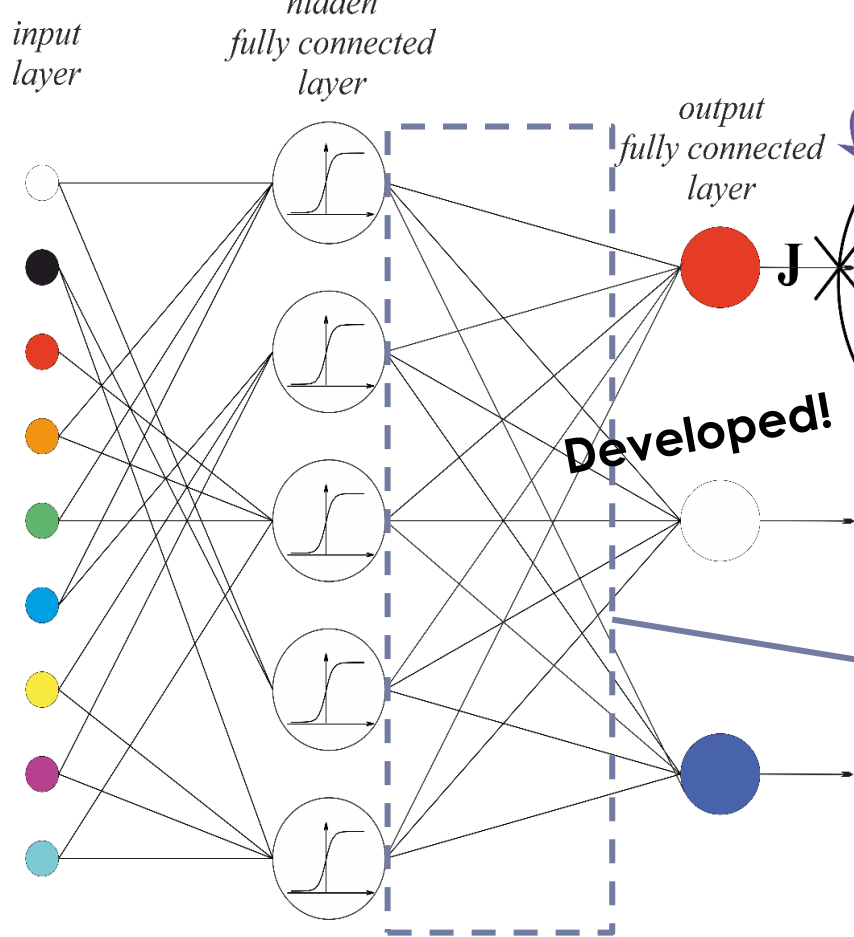


# Synapse: main idea

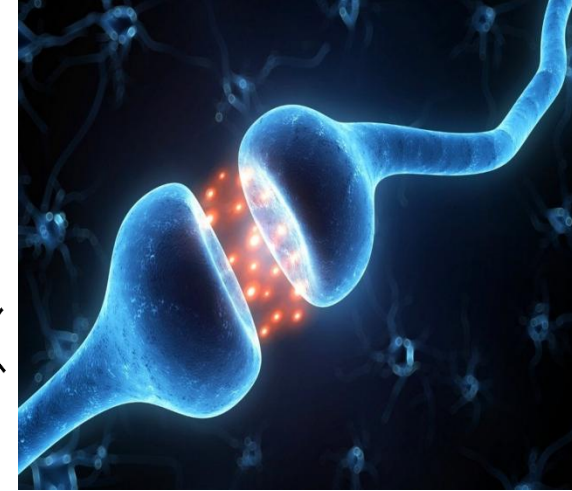
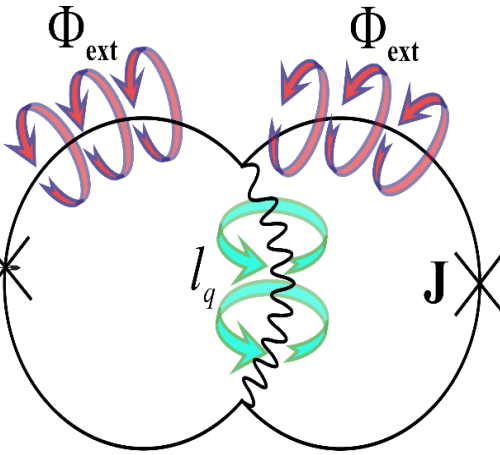
input layer

hidden fully connected layer

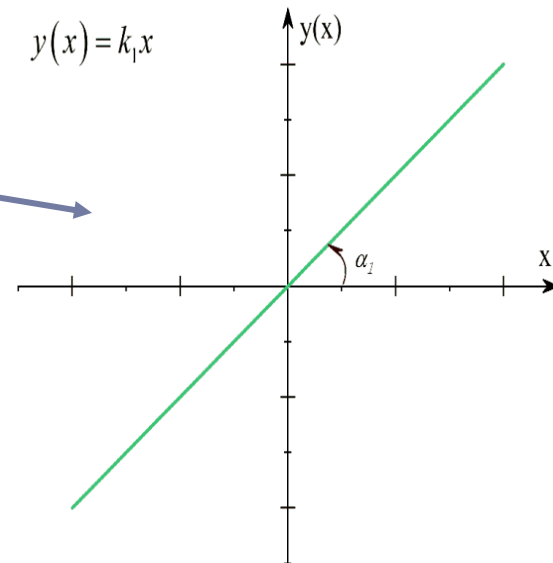
output fully connected layer



**Developed!**

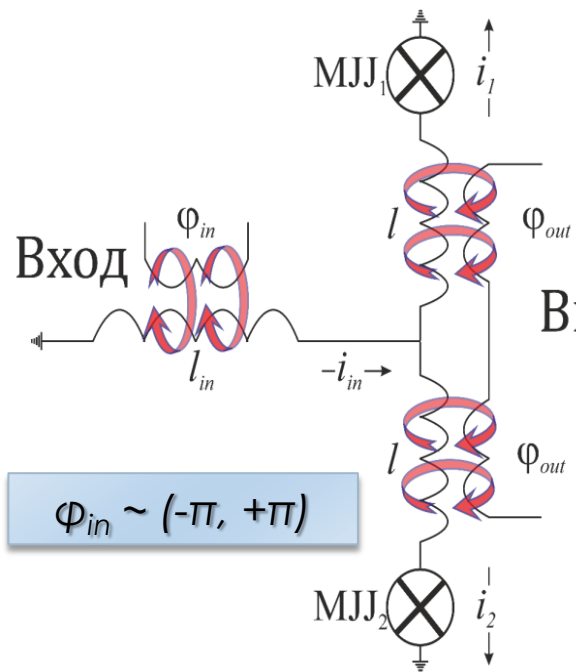


$$y(x) = k_1 x$$



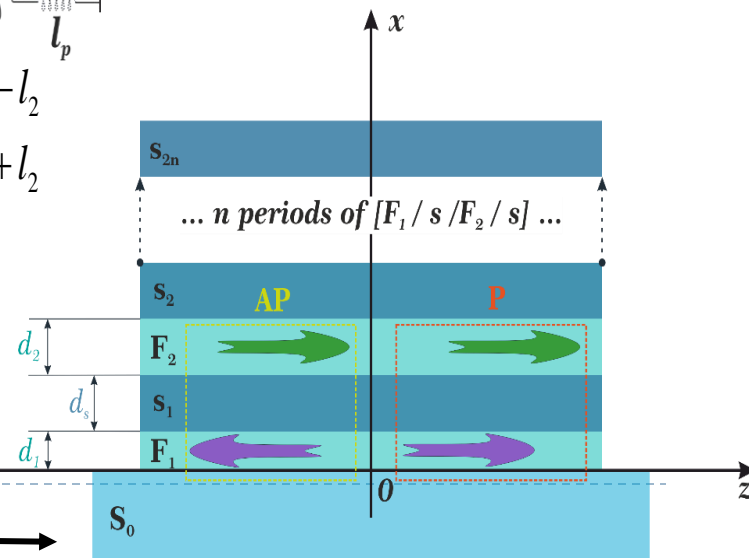
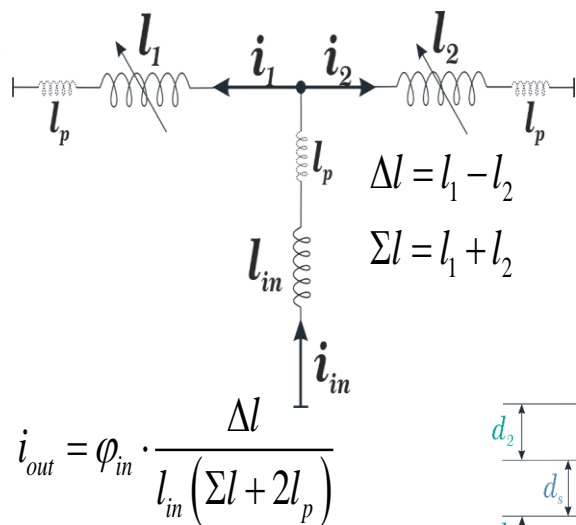
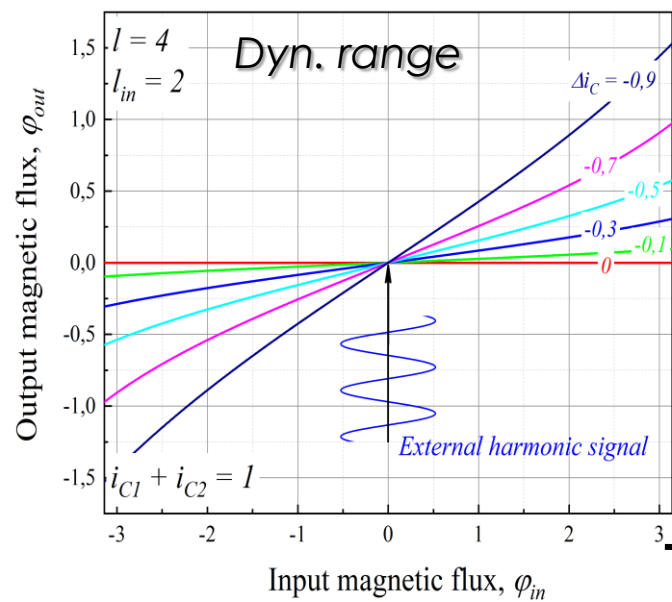
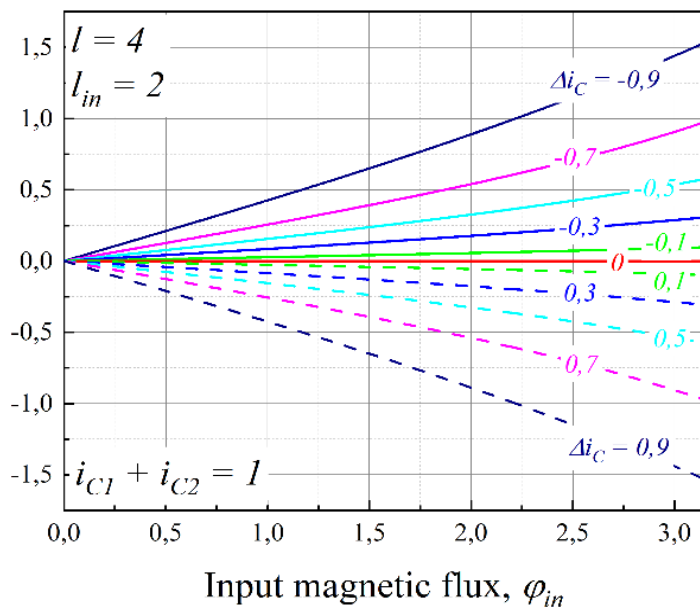


# Synapse: realization



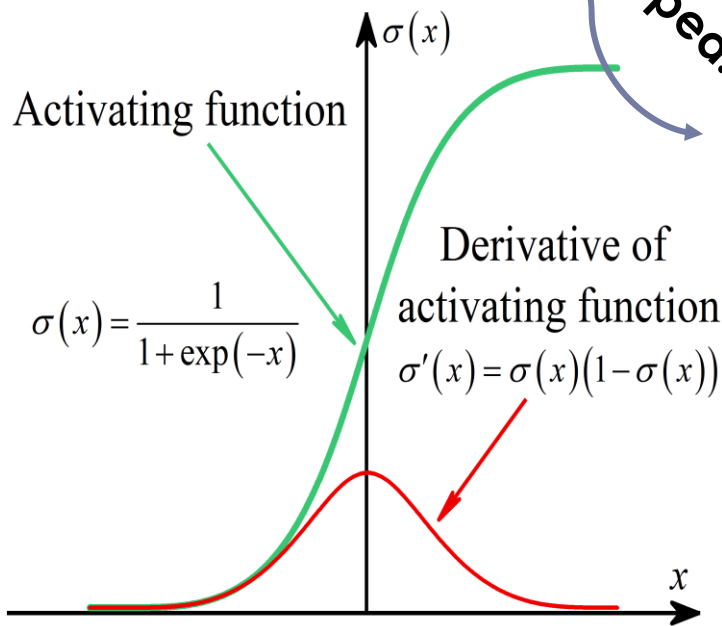
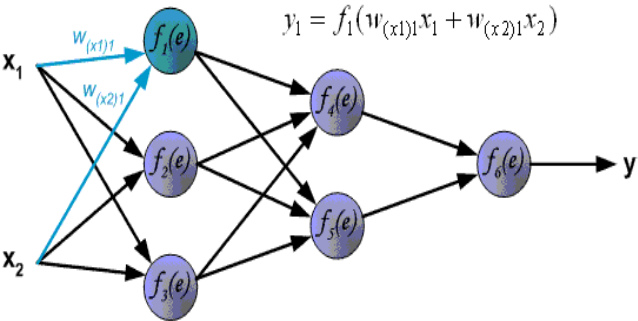
$$\varphi_{out} = -2\psi = (i_1 - i_2)l$$

Output magnetic flux,  $\varphi_{out}$

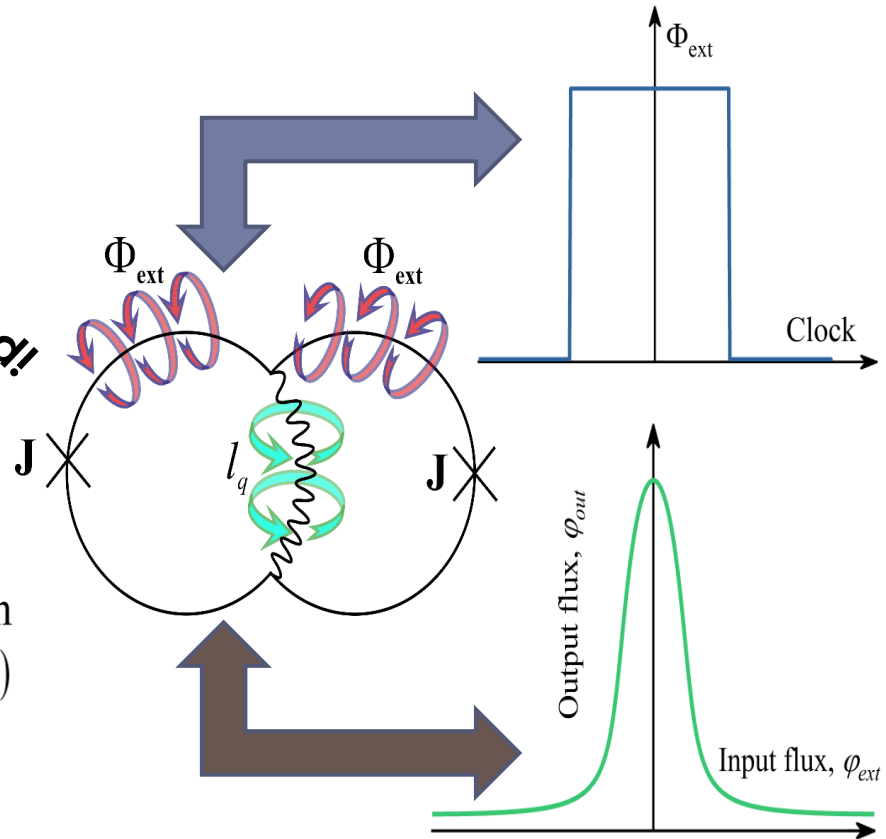


# Learning cell: main idea

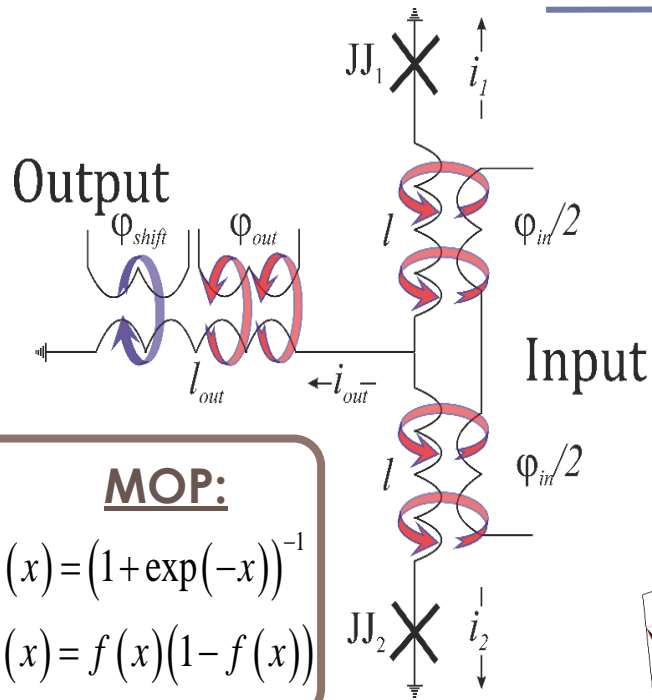
FP



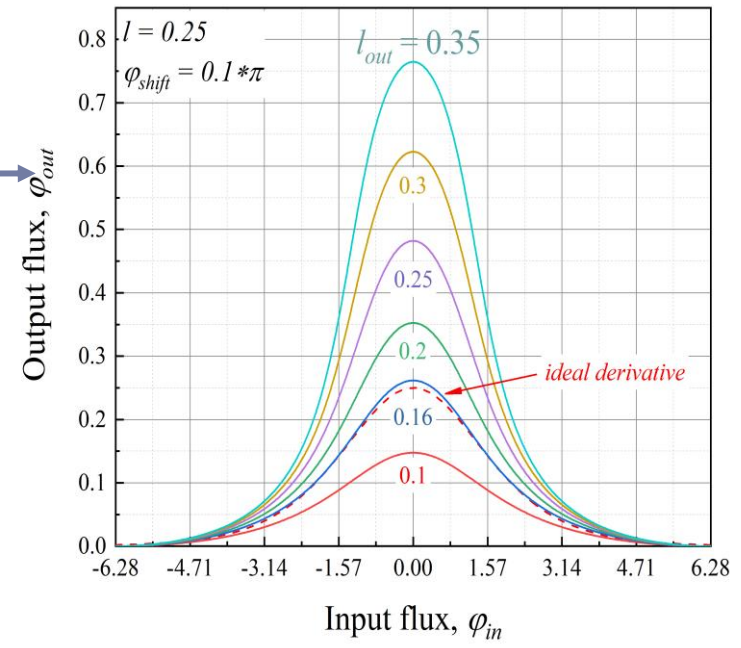
Developed!



# Learning cell: realization



$$\begin{cases} i_{1,2} = \frac{\Phi_{1,2}}{\Phi_0} + i_{C_{1,2}} \cdot \sin \varphi_{1,2} \\ i_{out} + i_1 + i_2 = 0 \\ i_1 l + \varphi_1 + \frac{\varphi_{in}}{2} = i_{out} l_{out} + \varphi_{shift} \\ i_2 l + \varphi_2 - \frac{\varphi_{in}}{2} = i_{out} l_{out} + \varphi_{shift} \end{cases}$$

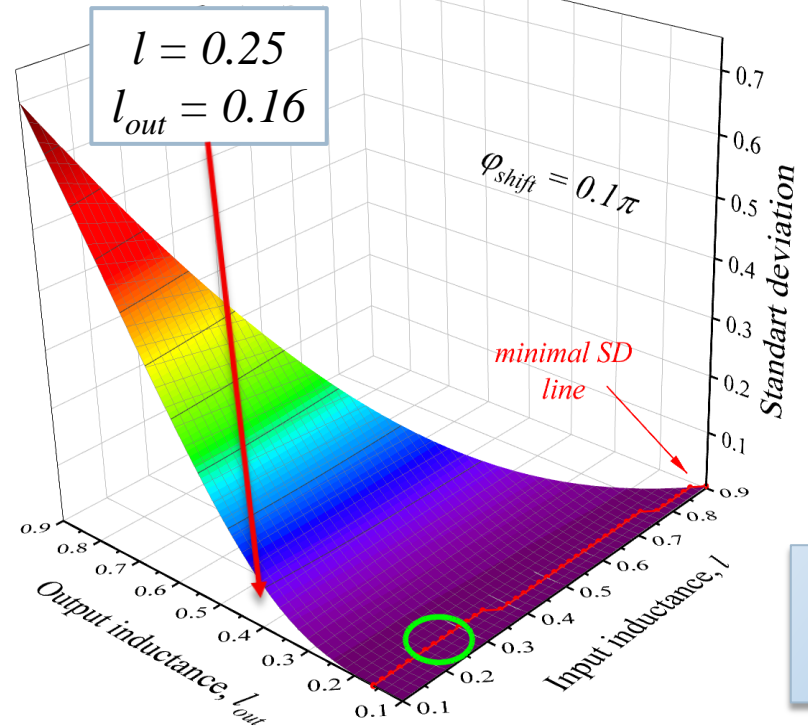


**MOP:**

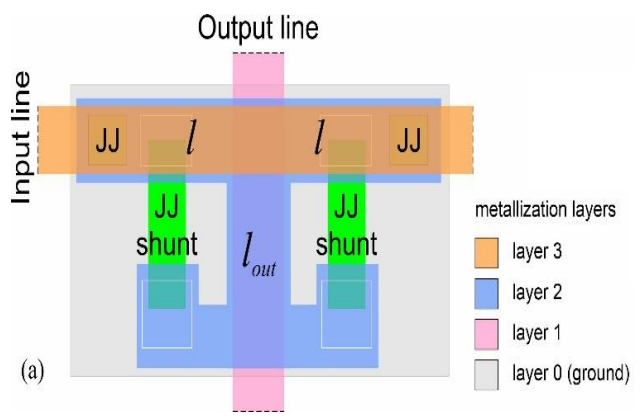
$$f(x) = (1 + \exp(-x))^{-1}$$

$$f'(x) = f(x)(1 - f(x))$$

## Optimization

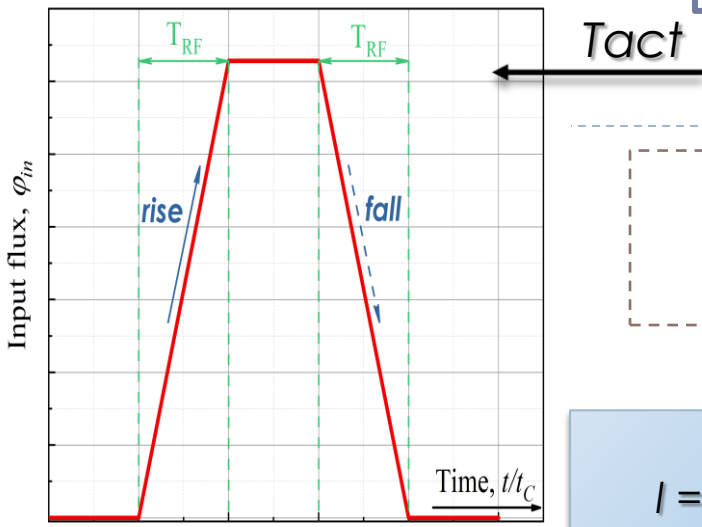


$$SD = \frac{\sum_{n=1}^N [f'_x(\varphi_{in}^{(n)}) - \varphi_{out}(\varphi_{in}^{(n)})]^2}{N}$$



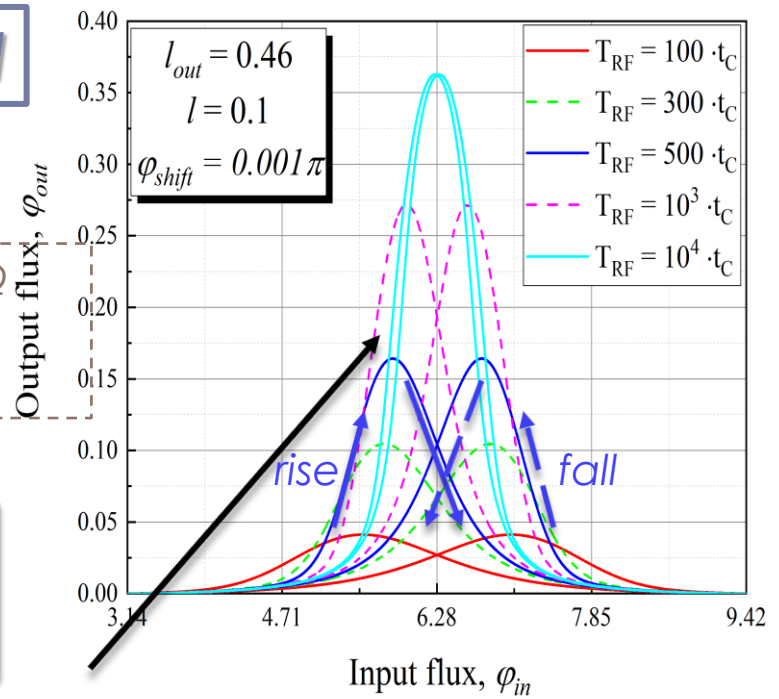
**Learning cell:  
10x10 μm**

# Learning cell

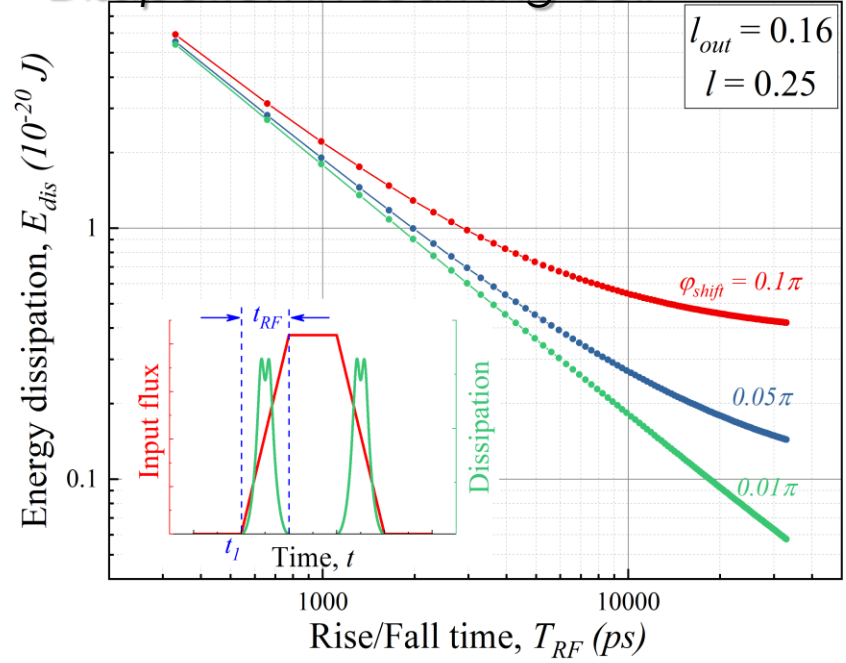


$I_C = 100 \mu A$   $R_N = 1 \Omega$   
 $T_{RF} = 33 ns$   
 $E_{dis} \approx 1 zJ$

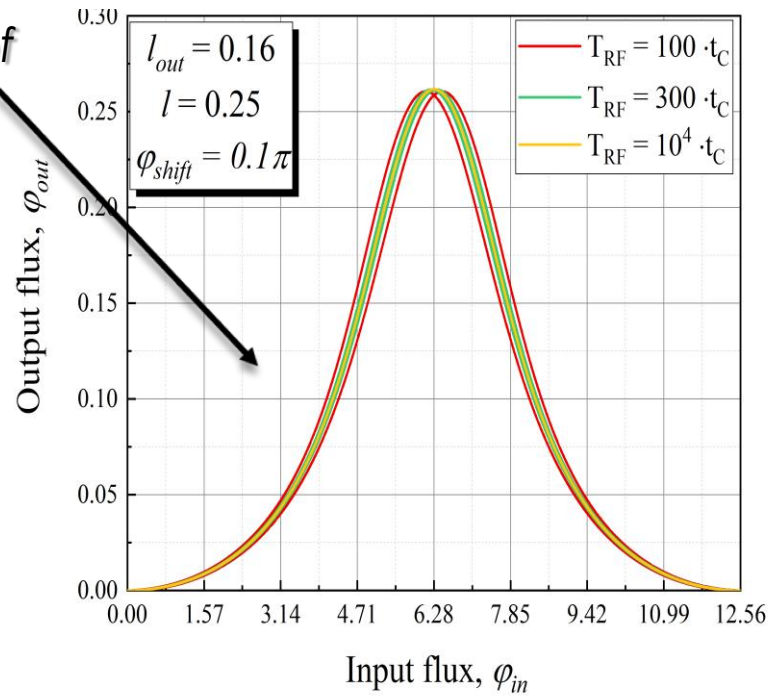
$t \approx 3.3 ns$   
 $l = 0.25$   $l_{out} = 0.16$   
 $E_{dis} \approx 4 - 60 zJ$



## Dissipation in Learning cell

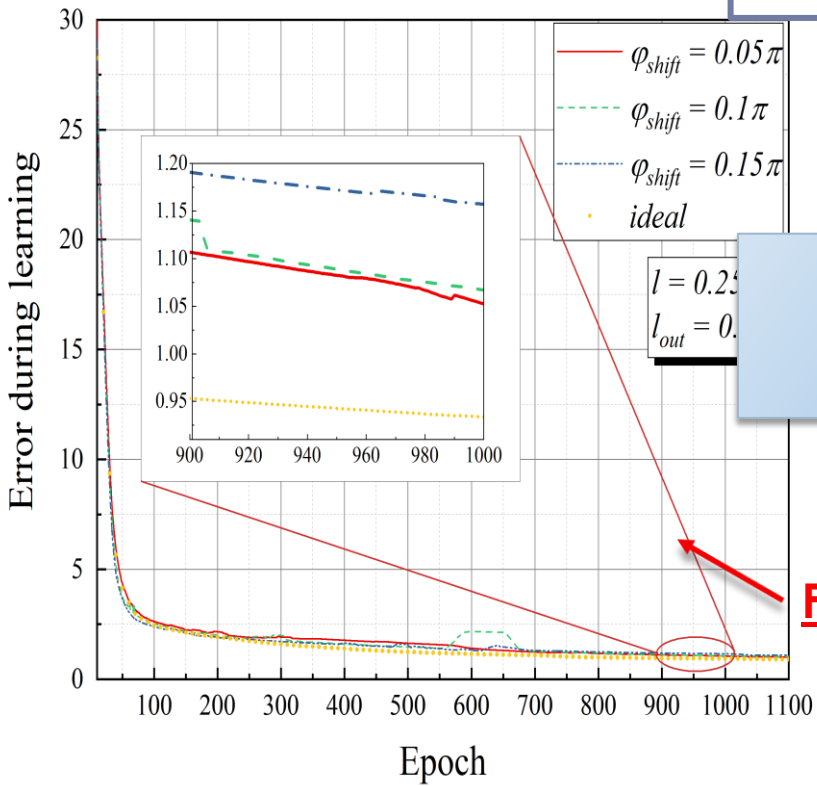
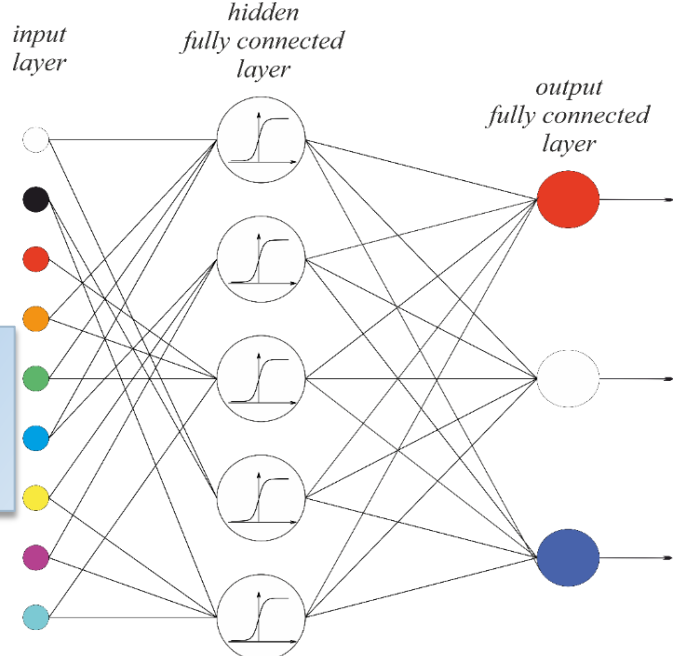


## Impact of $\varphi_{shift}$





# Learning cell

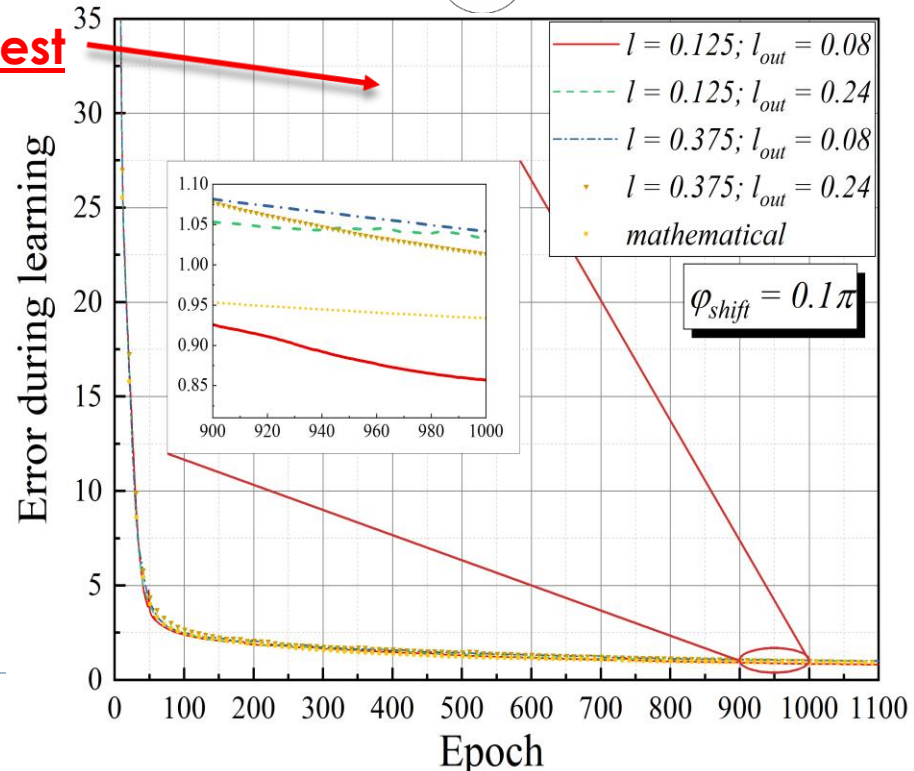


$t_{epoch} \approx 1 \text{ ns}$

$E_{dis} \approx 10 \text{ zJ}$

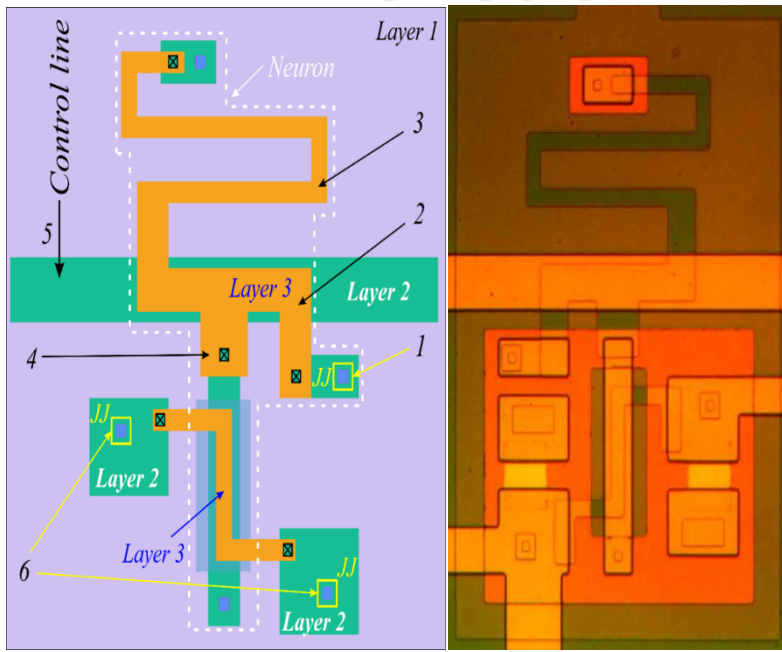
## Fisher test

A perceptron network of 16 neurons was modeled:  
 input layer – 4 neurons,  
 hidden layer – 9 neurons,  
 output layer – 3 neurons



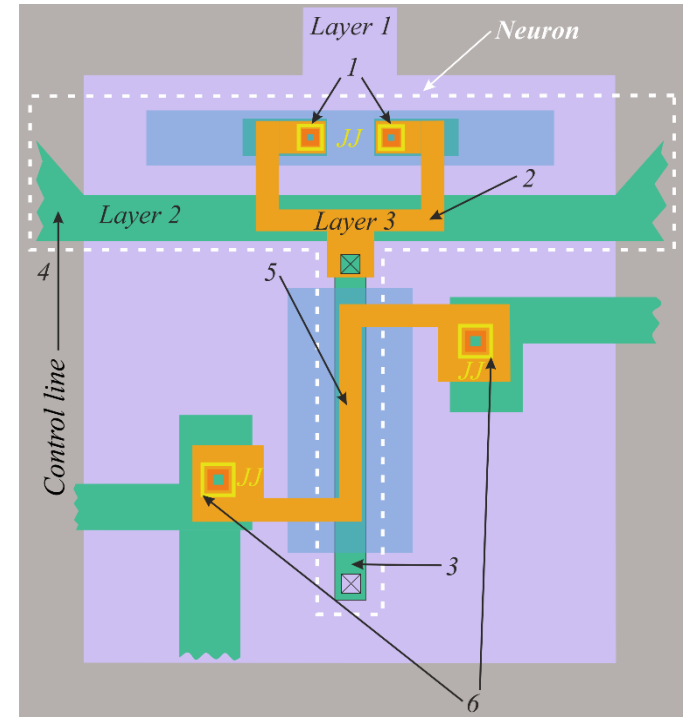
# Realization

## S-neuron

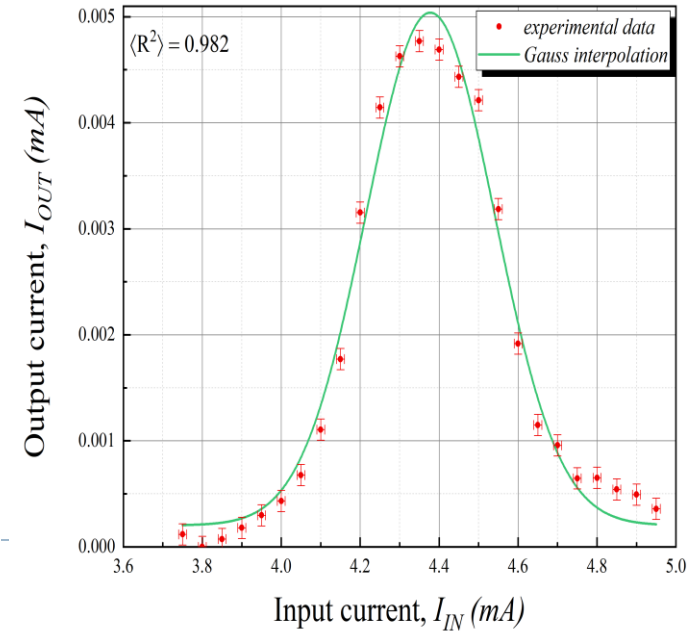
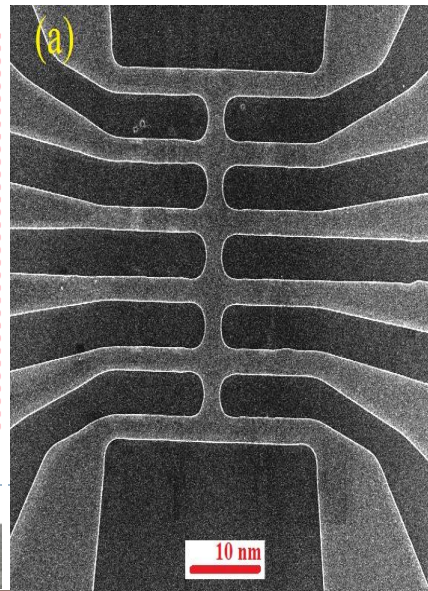
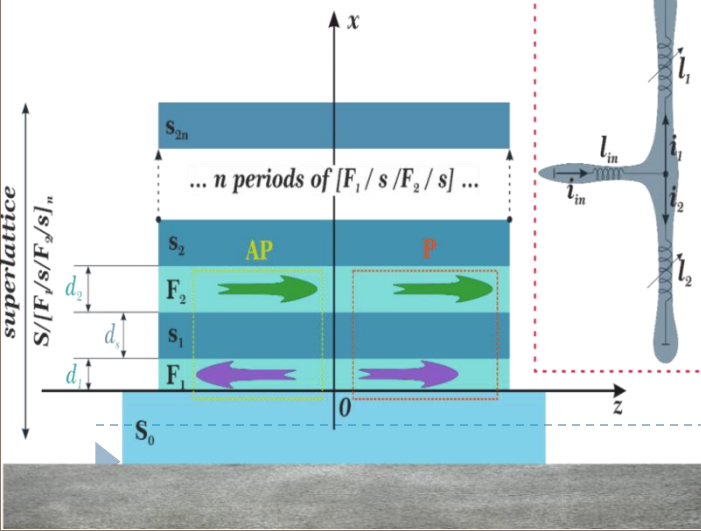


Thanks for  
V.M.K.  
&  
A.S.S.  
groups!

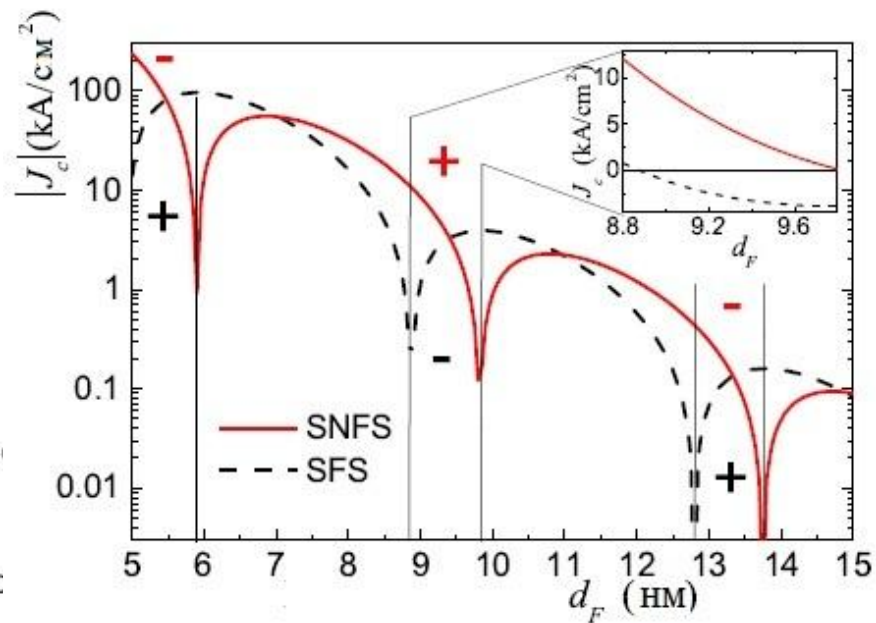
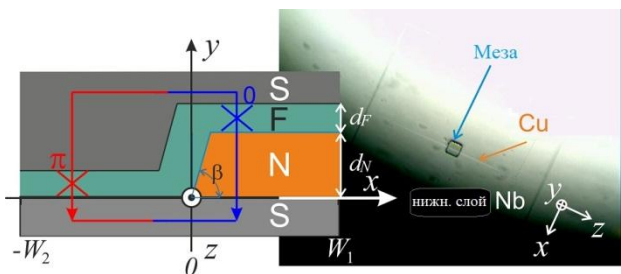
# G-neuron



## Ind. synapse

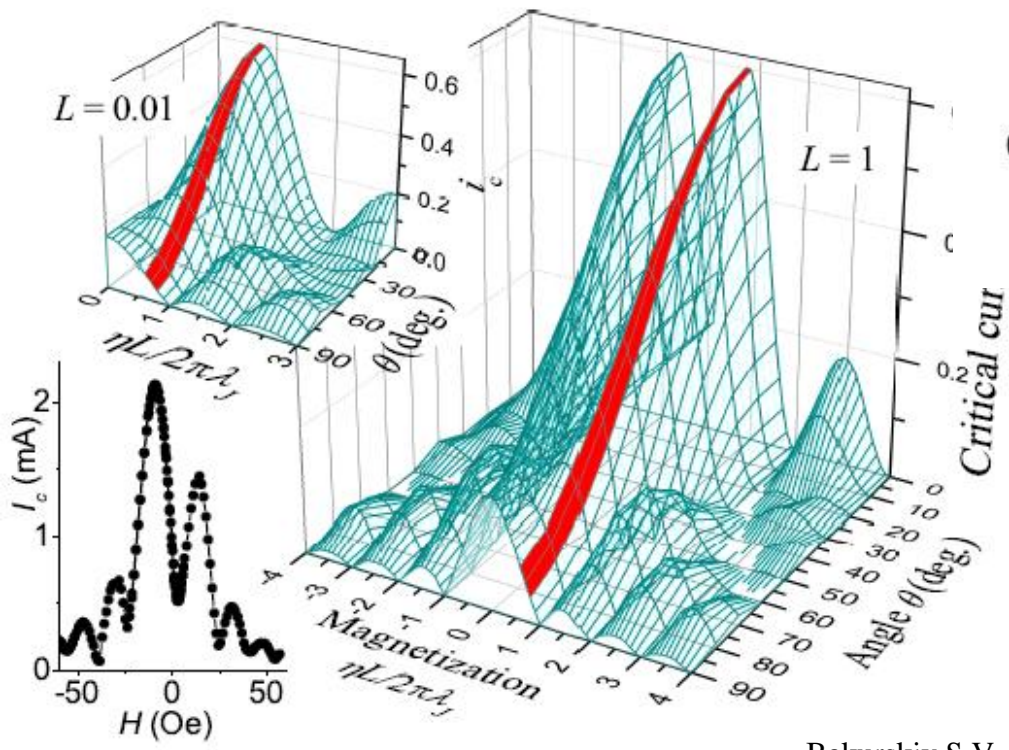


# Magnetic rotary valve (thanks to A.A.G. and V.V.R. groups)



**SF-NFS** → **SIsF-NFS**

- ✓ up to 100 GHz
- ✓ strong  $I_C$  modulation



Bakurskiy S.V., **Klenov N.V.**, Soloviev I.I., Bol'ginov V.V., Ryazanov V.V., Vernik I.V., Mukhanov O.A., Kupriyanov M.Yu., Golubov A.A. Theoretical model of superconducting spintronic SIsFS devices // Applied Physics Letters. — 2013. — Vol. 102. — P. 192603.

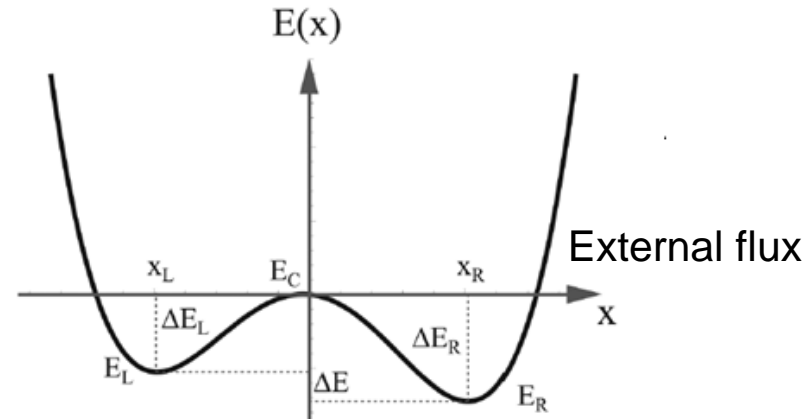
# Qubit as a neuron?

$$f(x) = \frac{1}{1 + e^{-x}}$$

$$\frac{dp_L}{dt} = -\Gamma_{LR}p_L + \Gamma_{RL}p_R,$$

$$\frac{dp_R}{dt} = -\Gamma_{RL}p_R + \Gamma_{LR}p_L,$$

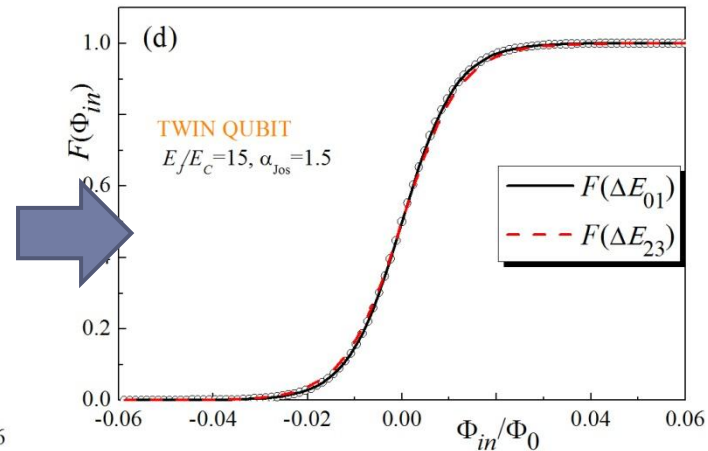
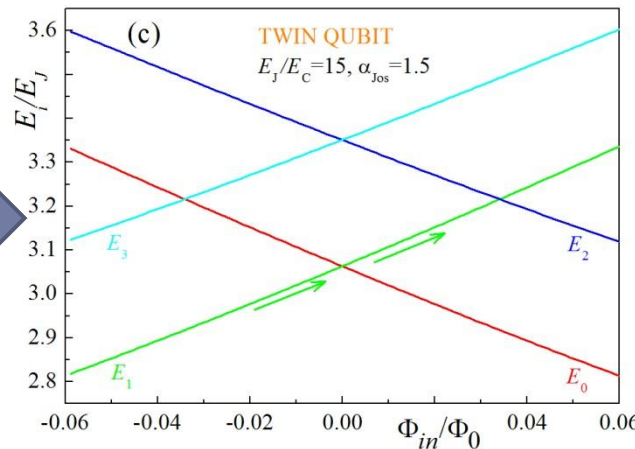
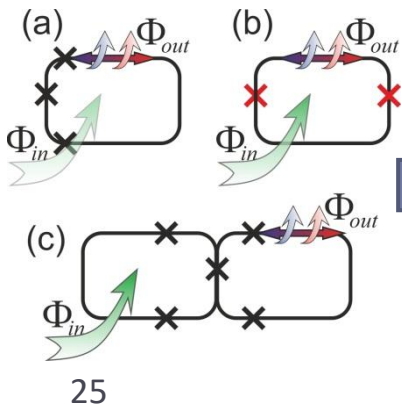
$$\frac{dp_L}{dt} = -(\Gamma_{LR} + \Gamma_{RL})p_L + \Gamma_{RL}$$



$$p_L = \left(1 - \frac{\Gamma_{RL}}{\Gamma_{LR} + \Gamma_{RL}}\right) e^{-(\Gamma_{LR} + \Gamma_{RL})t} + \frac{\Gamma_{RL}}{\Gamma_{LR} + \Gamma_{RL}}$$

$$p_L = \frac{\Gamma_{RL}}{\Gamma_{LR} + \Gamma_{RL}} = \frac{1}{1 + \Gamma_{LR}/\Gamma_{RL}}$$

$$\Gamma = \frac{\omega_0}{2\pi} e^{-\frac{\Delta U}{k_B T}} \quad \Rightarrow \quad p_L = \frac{1}{1 + e^{\frac{\Delta E}{k_B T}}}$$



N. V. Klenov, et al. *Low Temperature Physics*, 45(7):769–774, 2019.

A. V. Bogatskaya, N. V. Klenov, et al. *Laser Physics Letters*, 16(5):056006, 2019.

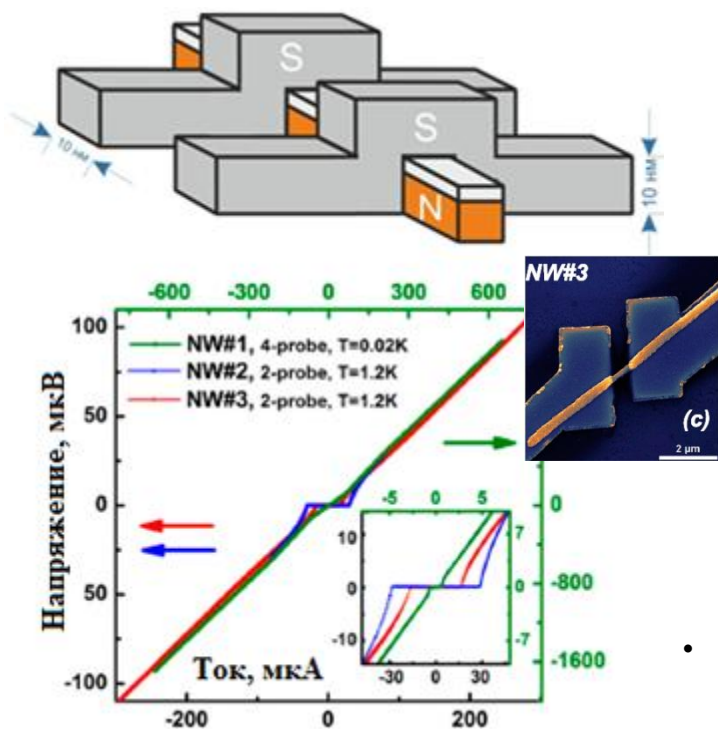


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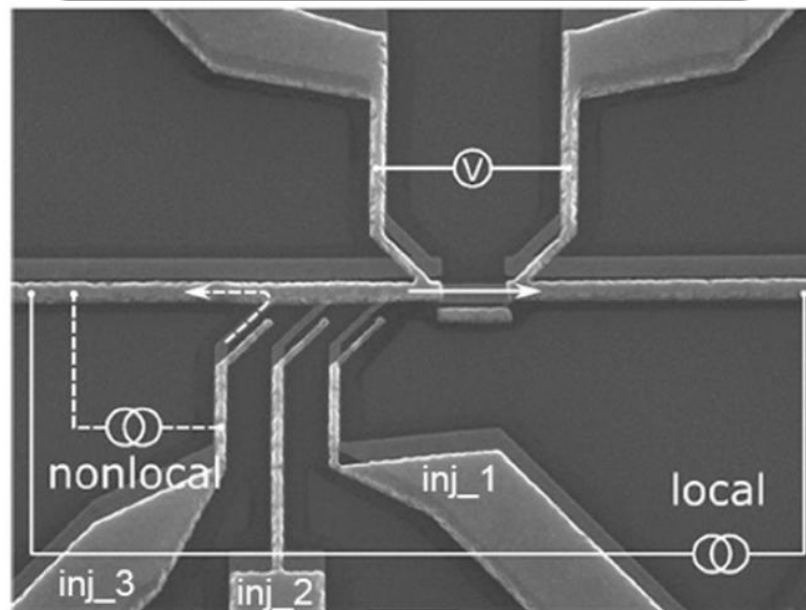
**THANK YOU FOR  
YOUR ATTENTION**

# Практические реализации: уменьшение размеров базовых элементов (I)

**Научная Новизна.** Созданы и апробированы методики для анализа процессов переноса заряда в компактных джозефсоновских элементах и фазовых батареях (с учетом особенностей влияния топологии при переходе к наноразмерным структурам), входящих как в состав ШП АЦП, так и в состав сигнального процессора, нейросетевого и квантового блока обработки сигнала

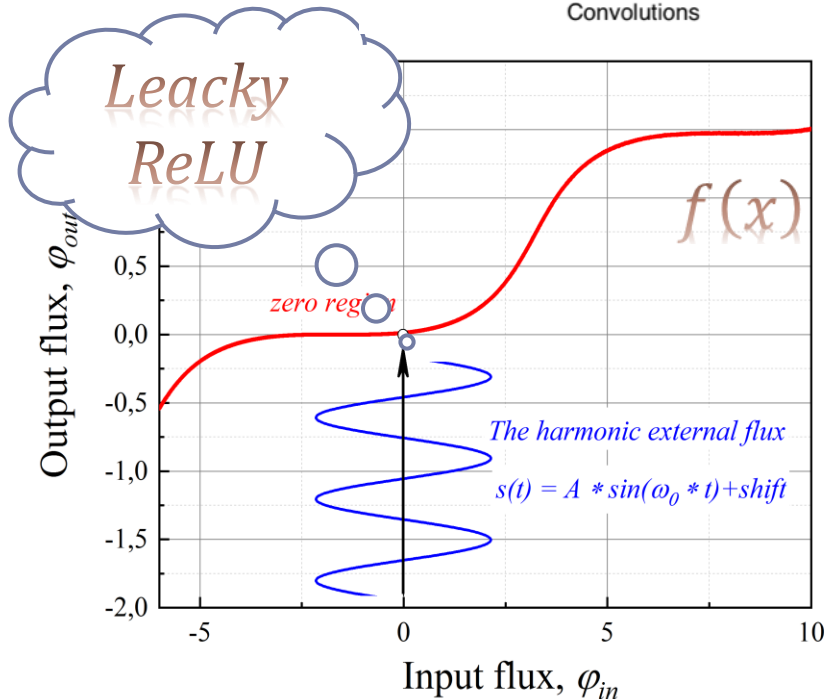
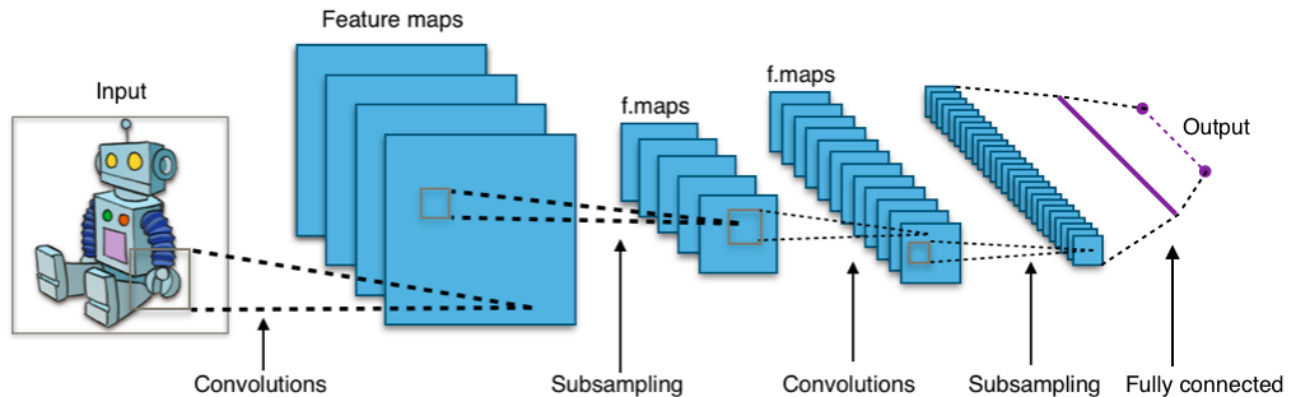


Отработка технологических решений



- Golikova T.E., Hubler F., Beckmann D., **Klenov N.V.**, Bakurskiy S.V., Kupriyanov M.Yu., Batov I.E., Ryazanov V.V. Critical current in planar SNS Josephson junctions // JETP Letters. — 2013. — Vol. 96, no. 10. — P. 668–673.

# Сверхпроводниковый ReLU (Rectifier Linear Unit) сверточных ИНС

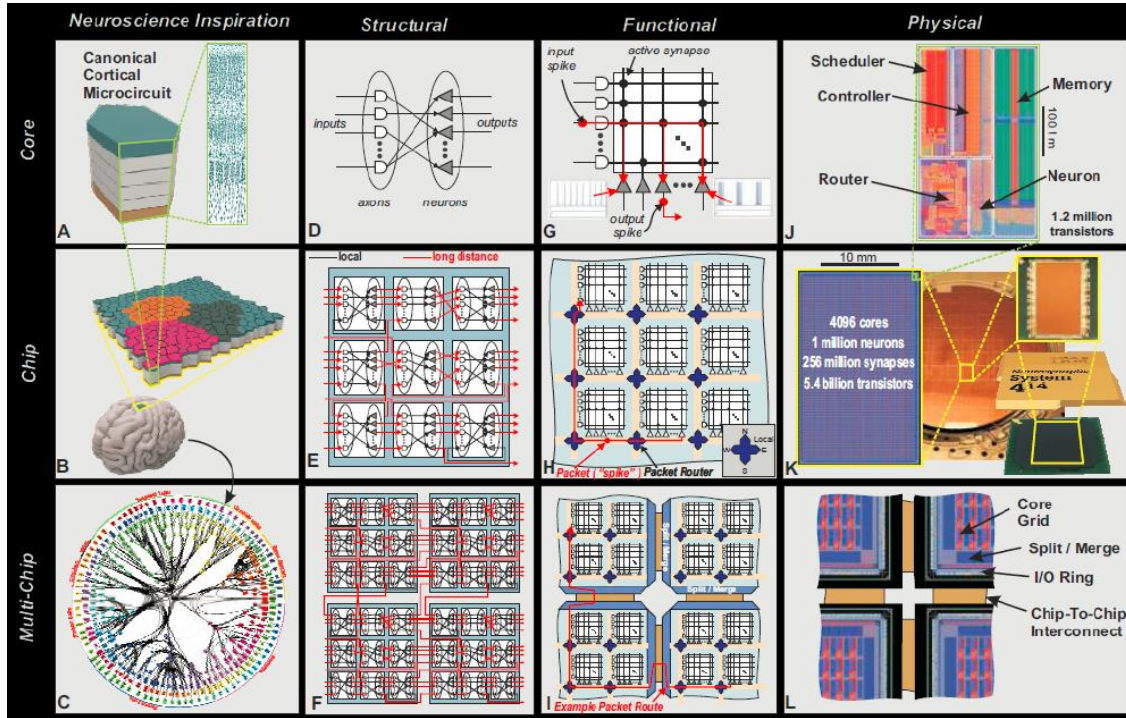


$f(x) \equiv \max\{0, x\}$  - математическая запись

Позволяет проводить обучение сверточной сети в несколько раз быстрее функций гиперболического тангенса или сигмоидной функции, без ущерба обобщающим свойствам сети

# Современные подходы к созданию элементной базы нейронных сетей

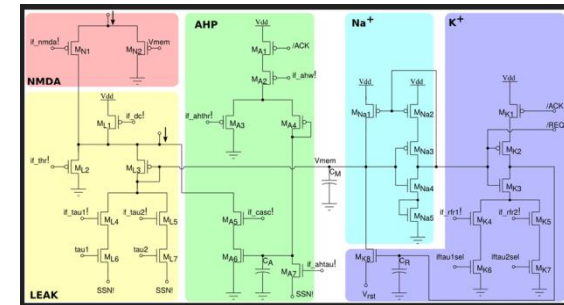
IBM TrueNorth



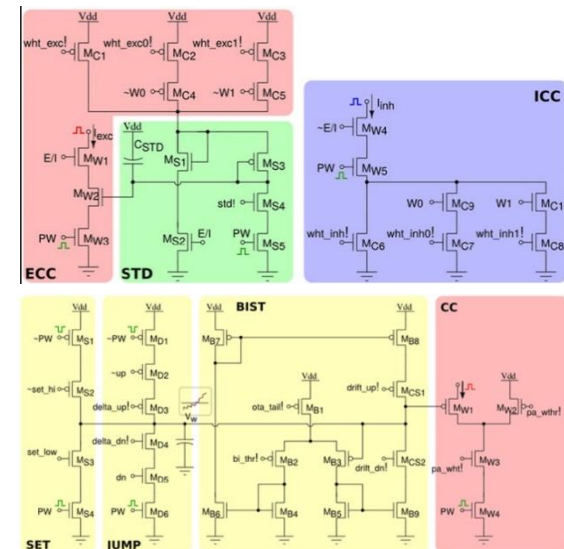
▪ Science 345, 668 (2014)

▪ Front Neurosci. 9, 141 (2015)

## КМОП нейрон



## Схемы для синапса





# Состояние исследований. Джозефсоновские структуры

## Основные физические эффекты:

➤ Эффекты Джозефсона

$$I = I_c \sin(\varphi)$$

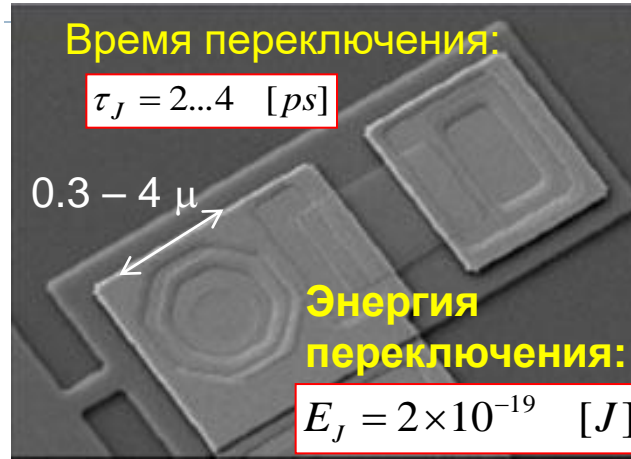
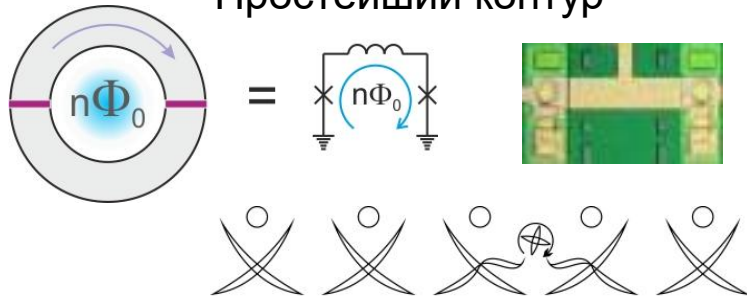
$$V = \frac{\eta}{2e} \frac{d\varphi}{dt} = \frac{\Phi_0}{2\pi} \frac{d\varphi}{dt}$$

➤ Квантование магнитного потока

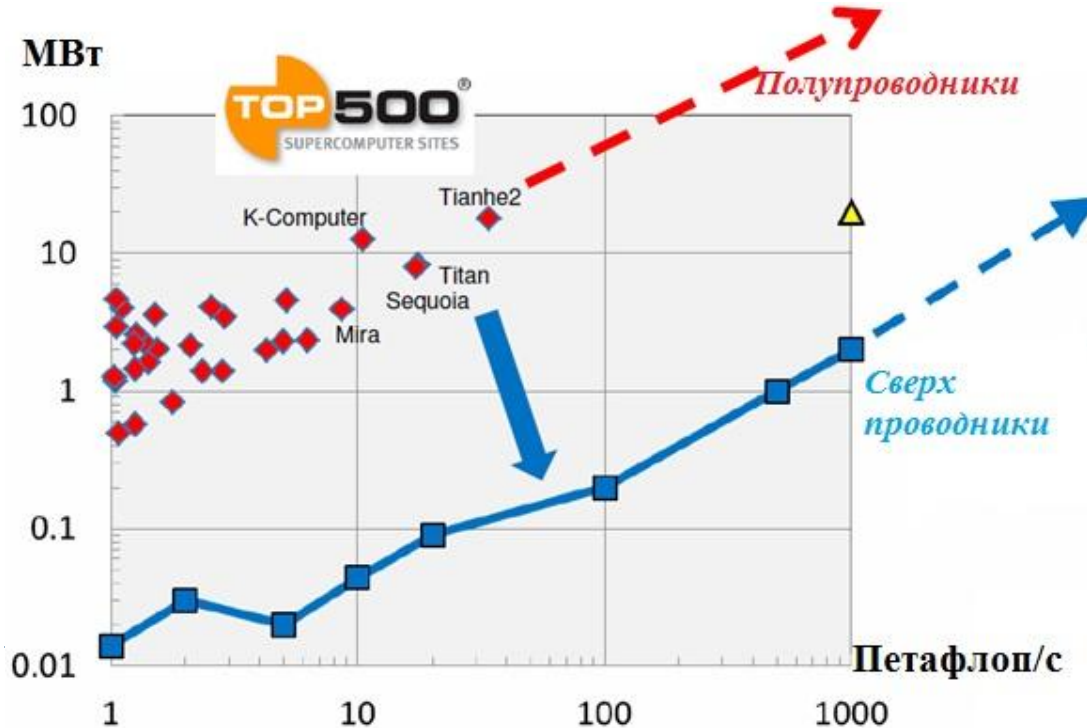
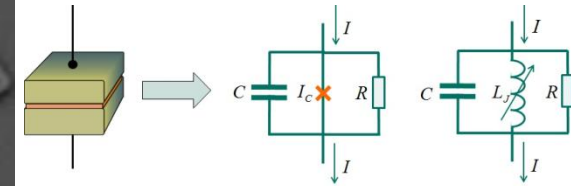
$$\Phi_0 = \frac{h}{2e} = \int V dt = 2.07 \text{ [мВ} \cdot \text{нс]}$$

или  $2.07 \times 10^{-15} \text{ [Вб]}$

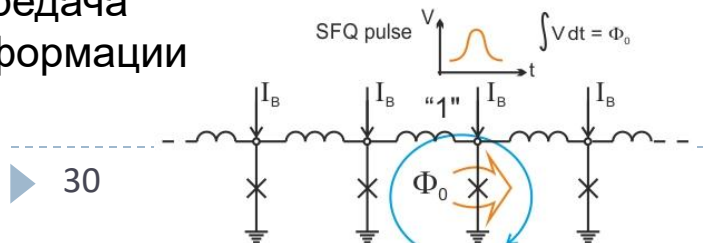
Простейший контур



Джозефсоновский контакт с резистивным шунтом



Передача информации

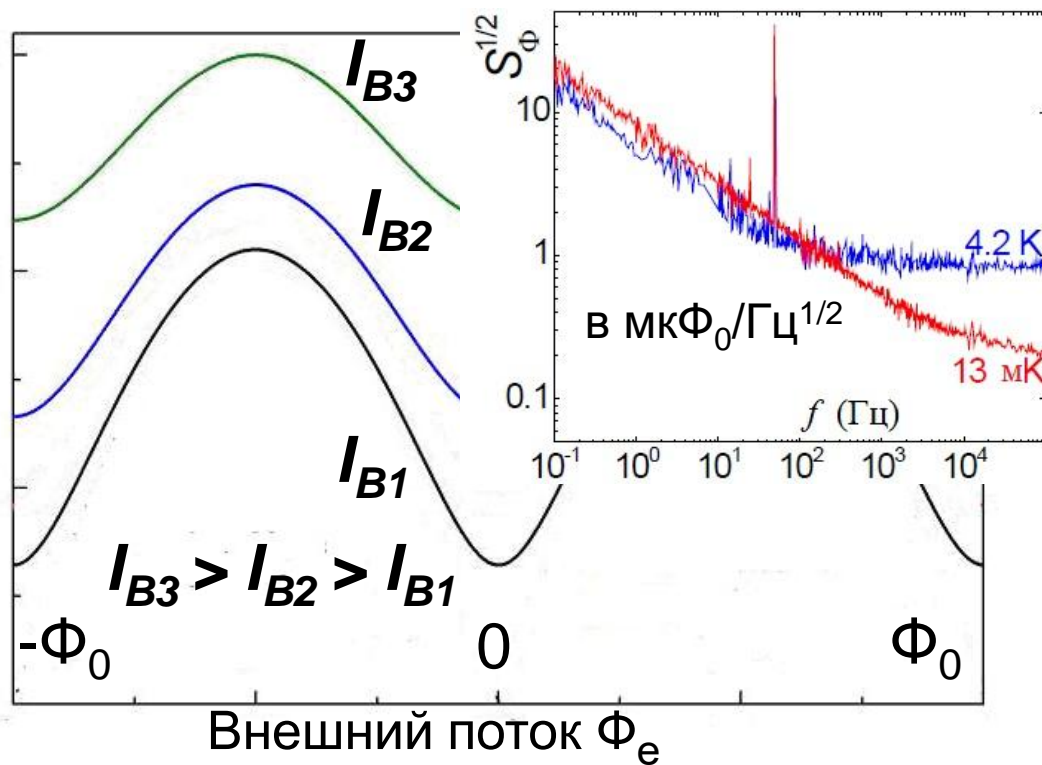
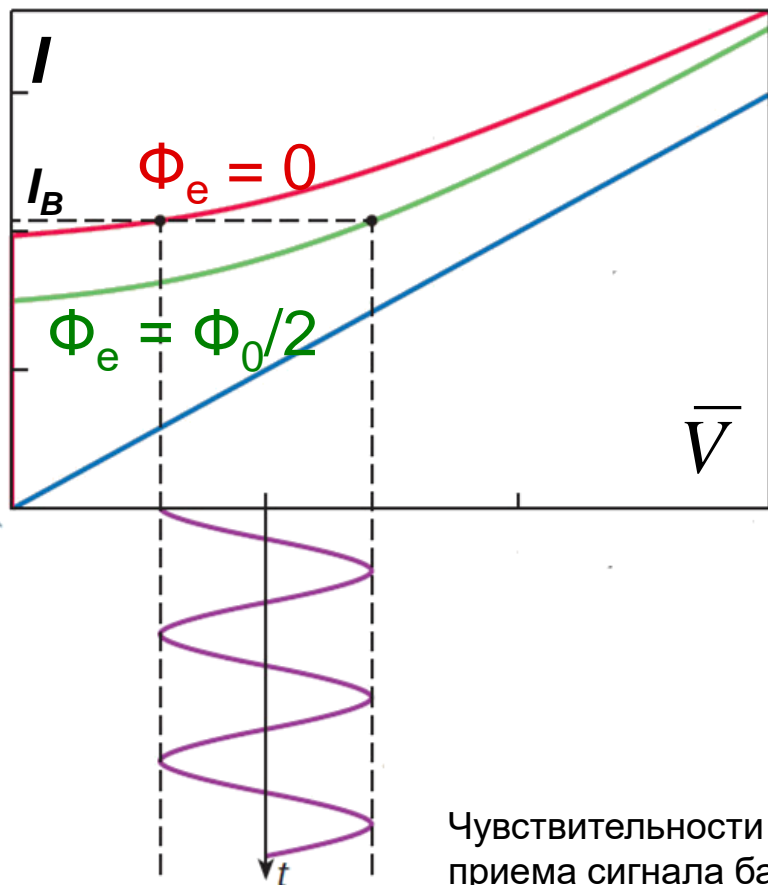
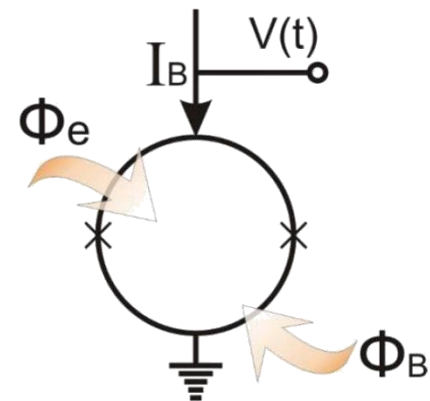


# Состояние исследований.

## Активный элемент приемной системы

R. C. Jaklevic, J. Lambe, A. H. Silver, and J. E. Mercereau "Quantum Interference Effects in Josephson Tunneling" *Phys. Rev. Letters* **12** (7), 159–160 (1964)

СКВИД – сверхпроводящий квантовый интерферометр

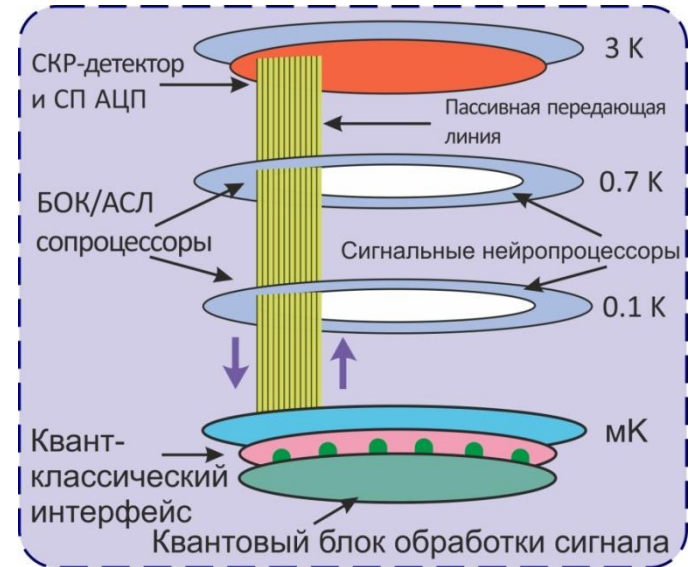


Чувствительности антенны, занимающей площадь  $3.3 \times 3.3 \text{ мм}^2$  достаточно для приема сигнала базовой станции сотовой связи на границе соты (35 км)

► **Общая идея работы:**

разрабатываем принципы создания «проблемных» элементов перспективной когнитивной широкополосной системы приема и обработки сигнала

Структура физ. реализации КШСС



**КШСС**

